



Quantum Critical Metals: From Loss of Quasiparticles to High T_c Superconductivity

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Rice University

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School on Exotic Superconductivity,
Cargèse, Corse, June 22, 2022

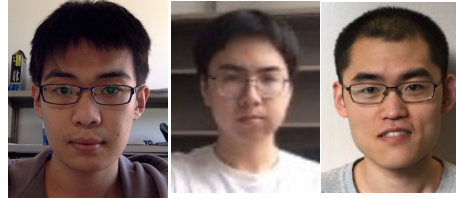


Rice University:

Haoyu Hu

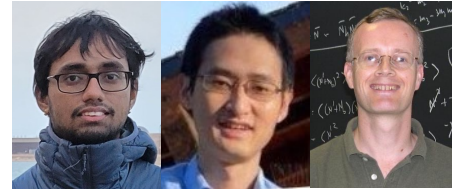
Lei Chen

Ang Cai



Rutgers University:

Jed Pixley



University of Florida:

Ananth Kandala

Lili Deng

Kevin Ingersent



Zhejiang University:

Stefan Kirchner



Vienna University of Technology:

Silke Paschen, Lukas Prochaska

Frank Steglich, Joe D. Thompson, Hilbert v. Löhneysen

Outline

- Quantum critical metals and the loss of quasiparticles
 - theoretical aspects, building on S. Paschen's lectures; in particular:
- High- T_c superconductivity out of the quantum critical metals

A. Kandala, H. Hu, QS, K. Ingersent, arXiv:2206.01174

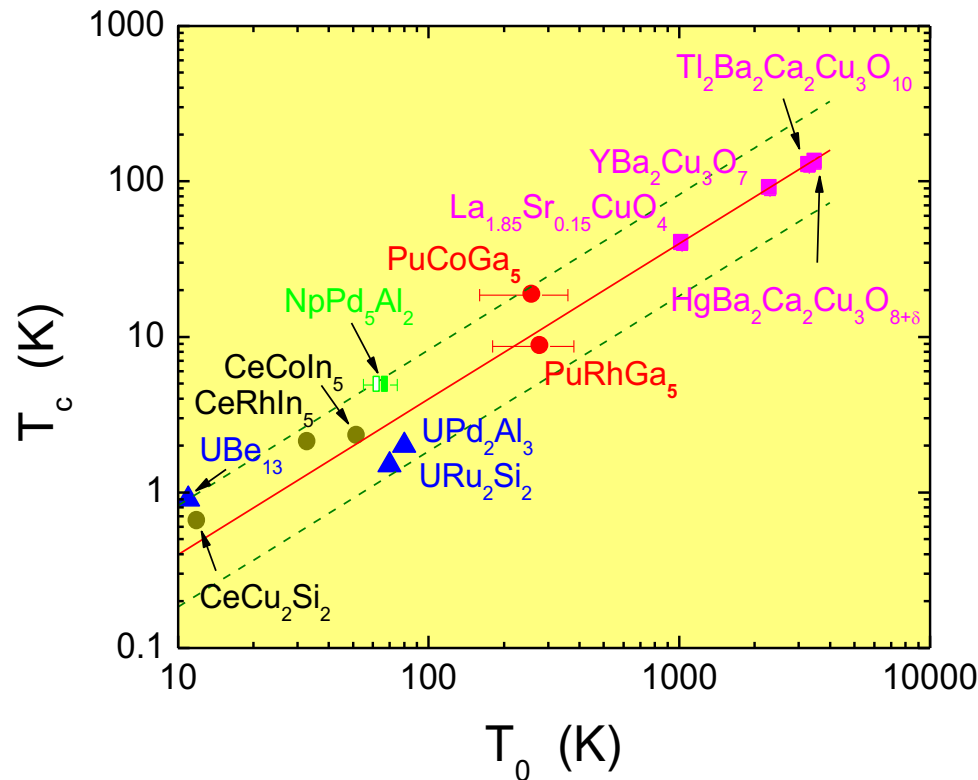
H. Hu, A. Cai, L. Chen, L. Deng, J. Pixley, K. Ingersent & QS,
arXiv:2109.13224

Notes and References

- “The many faces (phases) of strong correlations”, S. Paschen & QS, [Europhysics News \(EPN\) 52/4, 30-32 \(2021\)](#) (non-technical write-up).
- “Quantum phases driven by strong correlations”, S. Paschen & QS, [Nat. Rev. Phys. 3, 9-26 \(2021\)](#) (connecting different correlated platforms).
- “Heavy-electron quantum criticality and single-particle spectroscopy”, S. Kirchner, S. Paschen, Q. Chen, S. Wirth, D. L. Feng, J. D. Thompson, QS, [Rev. Mod. Phys. 92, 011002 \(2020\)](#) (large and small Fermi surfaces).
- “Quantum criticality and the Kondo lattice”, [arXiv:1012.5440](#); in “Understanding quantum phase transitions”, L. D. Carr, editor (CRC press, 2010) (a brief overview on the theoretical models and concepts).
- “Heavy fermions and quantum phase transitions”, QS and F. Steglich, [Science 329, 1161 \(2010\)](#) (an emphasis on the global phase diagram).
- “Quantum criticality in heavy-fermion metals”, P. Gegenwart, QS, F. Steglich, [Nat. Phys. 4, 186 \(2008\)](#) (an earlier comprehensive review).

Goalpost of the Talk

- Can, and how does, a quantum critical metal lacking quasiparticles lead to high- T_c superconductivity?



Courtesy
J. D. Thompson

Quantum Criticality

Quantum critical point

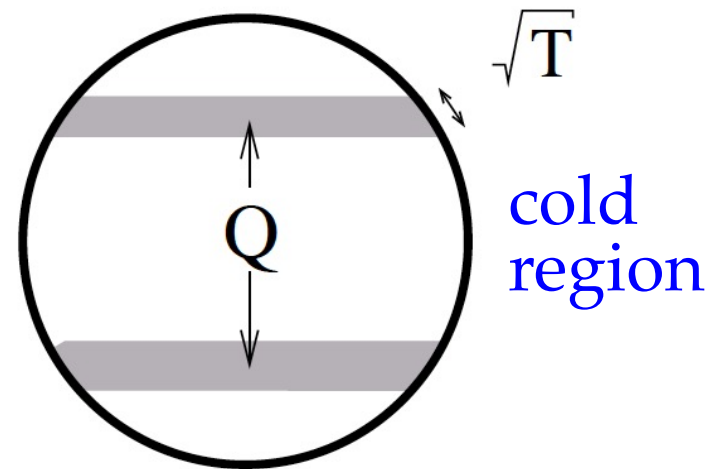
enhanced
entropy



unusual excitations;
emergent phases

Quantum Critical Metals

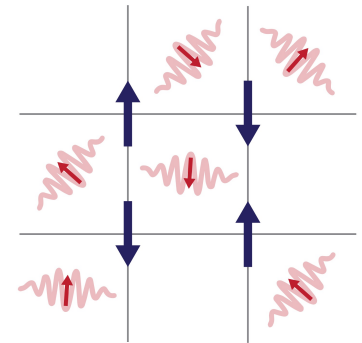
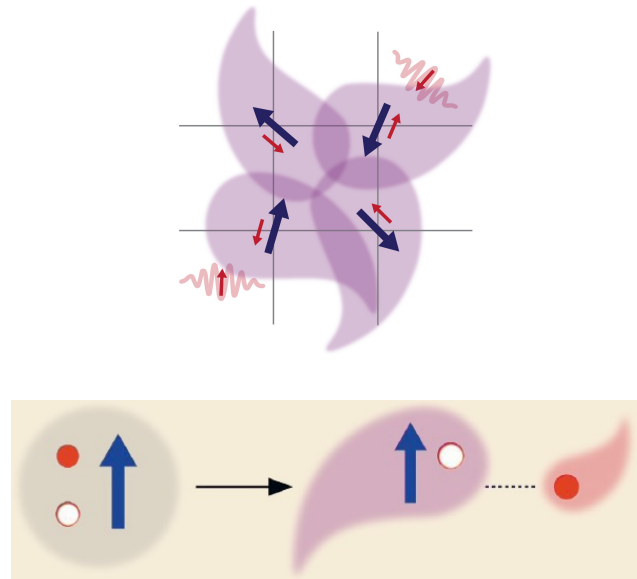
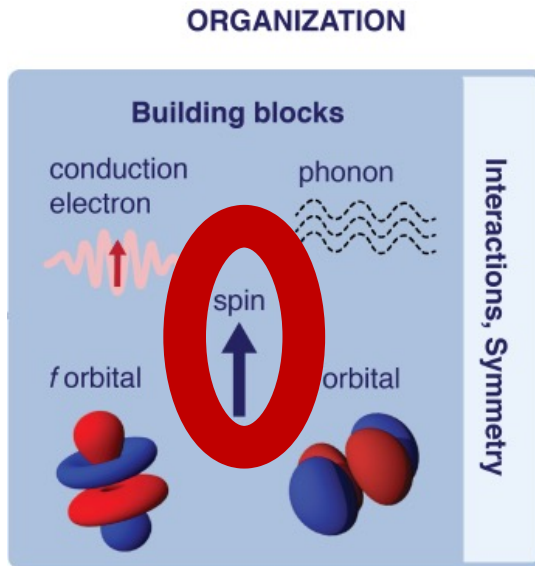
- Landau framework (Hertz, Millis)
 - Fluctuations of the order parameter
 - O.P. fluctuations leave well-defined quasiparticles (c.f., SDW QCP)



- Or beyond-Landau?
 - Are there critical modes beyond the order-parameter fluctuations?

Heavy Fermion Metals

Strong Coulomb repulsion \rightarrow spins are a part of the building blocks for the low-energy physics

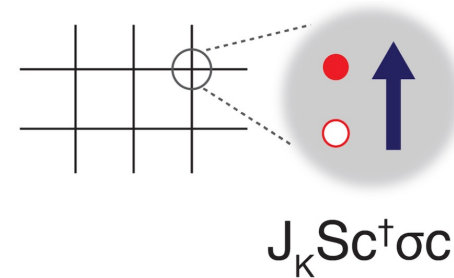


Introduction and status summary:

S. Paschen and QS, Nat. Rev. Phys. 3, 9 (2021)

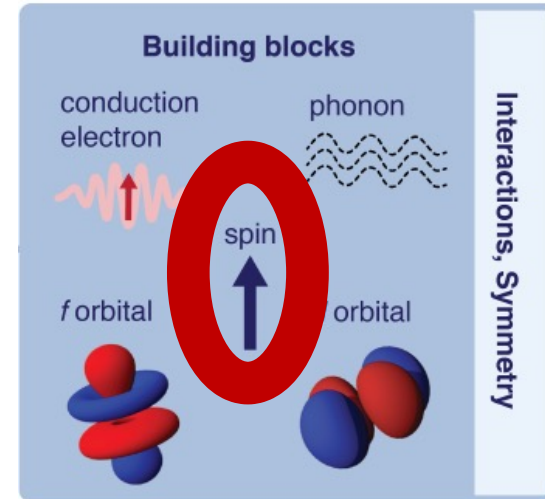
Kondo Lattice Systems

$$H = \sum_{ij} I_{ij} \mathbf{S}_i \cdot \mathbf{S}_j + \sum_{ij, \sigma} t_{ij} c_{i\sigma}^\dagger c_{j\sigma} + \sum_i J_K \mathbf{S}_i \cdot \mathbf{s}_{c,i}$$



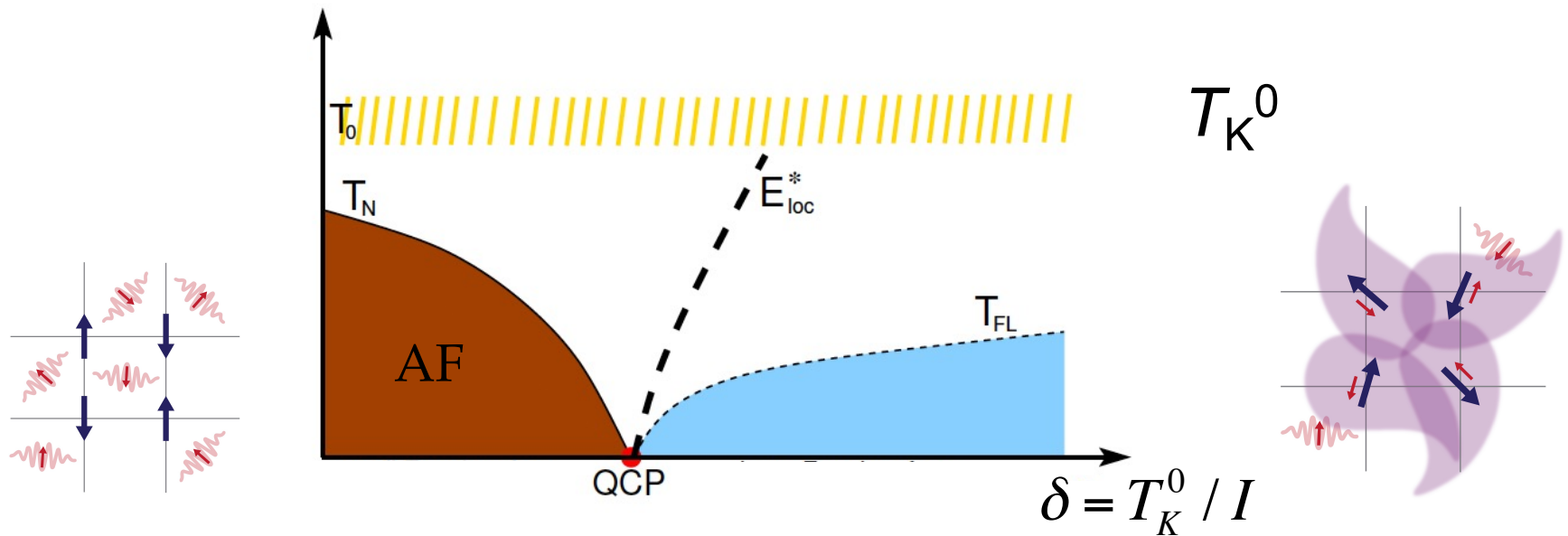
- Fate of local moments
 - end up fluctuating or forming order:
- Kondo entanglement,
- quantum magnetism, ...,

ORGANIZATION



Quantum Criticality from Kondo Destruction

Critical destruction of Kondo singlet
at the $T=0$ onset of antiferromagnetic order

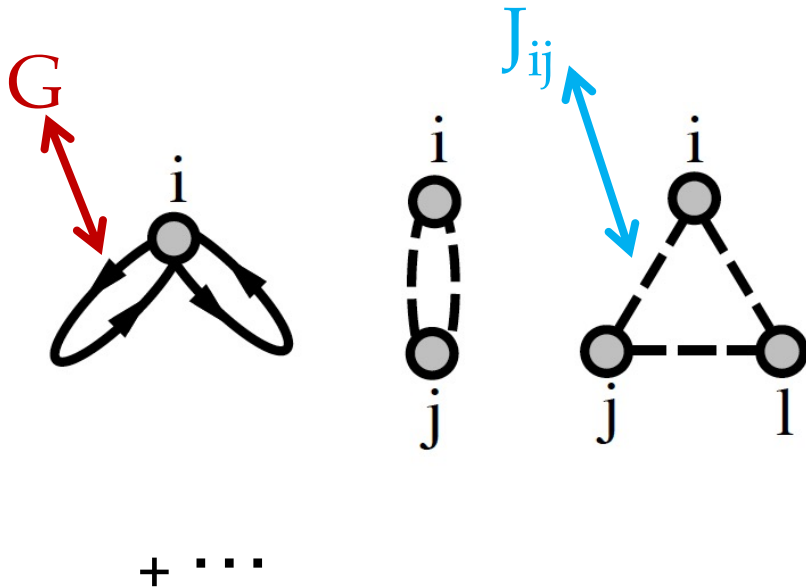


QS, S. Rabello, K. Ingersent & J. L. Smith, *Nature* 413, 804 (2001)

S. Kirchner, S. Paschen, Q. Y. Chen, S. Wirth, D. L. Feng,
J. D. Thompson, QS, *Rev. Mod. Phys.* 92, 011002 (2020)

Quantum Criticality from Kondo Destruction

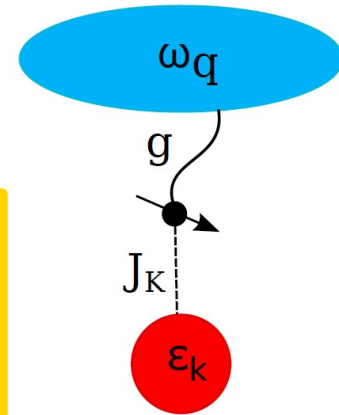
EDMFT:



Kondo lattice model



Bose-Fermi
Kondo model



QS & J. L. Smith, PRL 77, 3391 ('96);

J. L. Smith & QS, PRB 61, 5184 ('00);

R. Chitra & G. Kotliar, PRB 63,

115110 ('01)

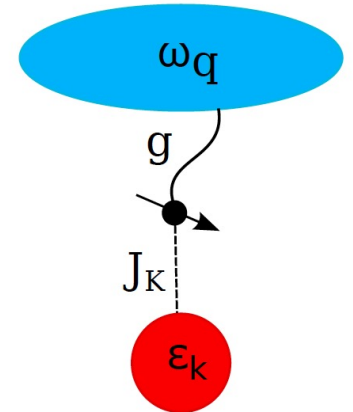
Quantum Criticality from Kondo Destruction

EDMFT:

Kondo lattice model



Bose-Fermi
Anderson / Kondo



$$S_{BFA} = \int_0^\beta d\tau \left[\sum_\sigma f_\sigma^\dagger \partial_\tau f_\sigma + U n_{d,\uparrow} n_{d,\downarrow} - \mu n_d \right] - \int_0^\beta d\tau d\tau' \sum_\sigma f_\sigma^\dagger(\tau) V^2 G_{c,0}(\tau - \tau') f_\sigma(\tau')$$

$$+ \frac{1}{2} \int_0^\beta d\tau \int_0^\beta d\tau' \sum_{\alpha \in \{x,y,z\}} : S^\alpha : (\tau) [\chi_0^\alpha]^{-1}(\tau - \tau') : S^\alpha : (\tau') + \int_0^\beta d\tau h_{loc} S^z$$

QS & J. L. Smith, PRL 77, 3391 ('96);

J. L. Smith & QS, PRB 61, 5184 ('00);

R. Chitra & G. Kotliar, PRB 63,

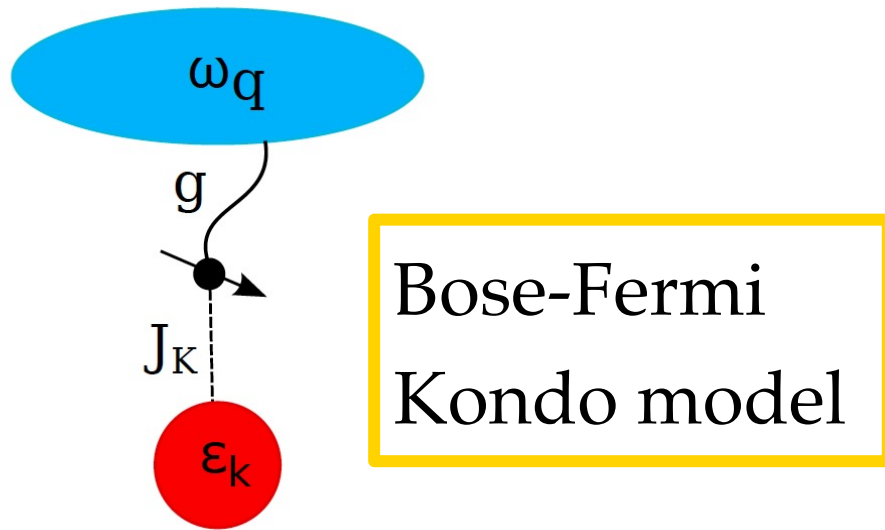
115110 ('01)

$$\chi_{loc}^\alpha(i\omega) = \sum_q \frac{1}{I_q + M^\alpha(i\omega)}$$

$$h_{loc} = I_Q \langle S^z \rangle$$

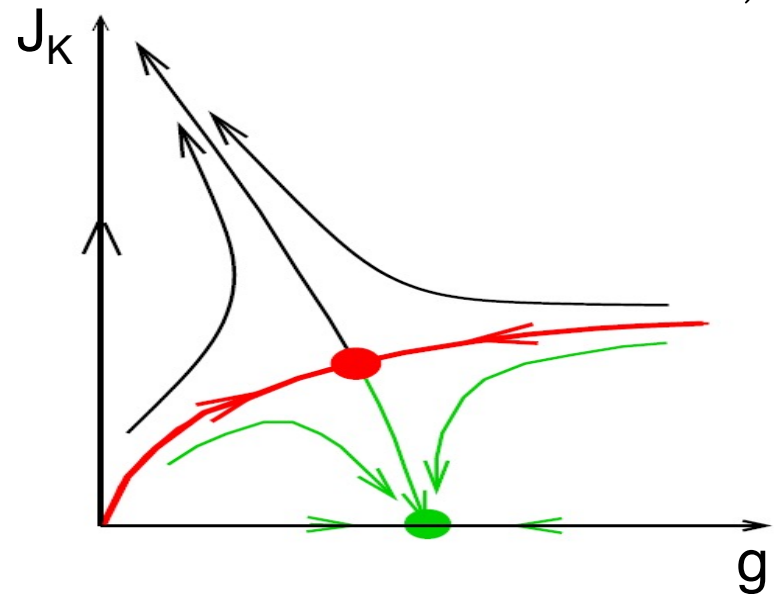
$$G_{c,loc}(i\omega) = \sum_k \frac{1}{i\omega - \epsilon_k - \Sigma_c(i\omega)}$$

Quantum Criticality from Kondo Destruction



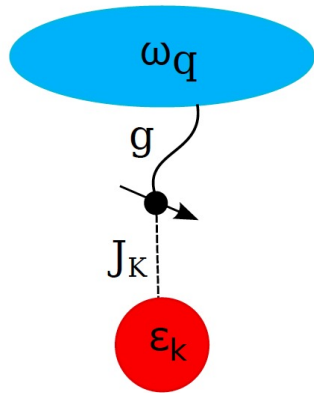
RG via ϵ -expansion

($1-\epsilon$: power-law spectrum of the bosonic bath)

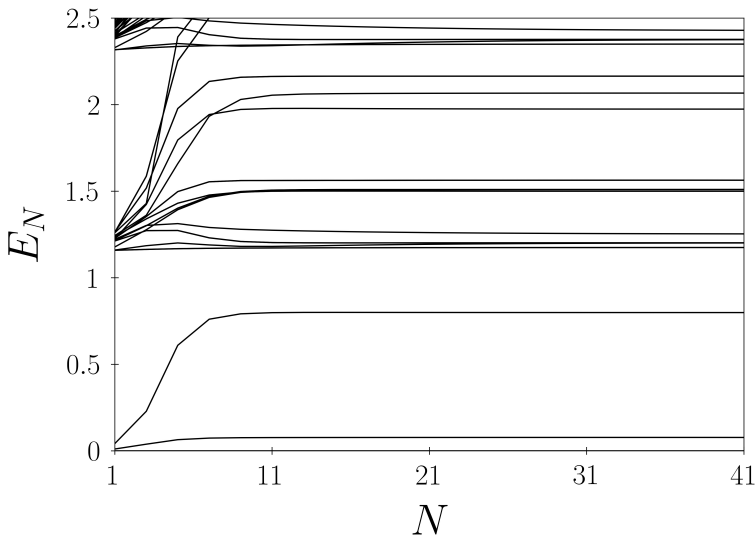


- QS & J.L. Smith, PRL 77, 3391 ('96); QS, J.L. Smith & K. Ingersent, IJMPB 13, 2331 (1999);
J. L. Smith & QS, EPL 45, 228 ('99), cond-mat/9705140;
A.M. Sengupta, PRB 61, 4041 ('00), cond-mat/9707316;
L. Zhu & QS, PRB 66, 024426 ('02); G. Zarand & E. Demler, PRB 66, 024427 ('02)

Loss of Quasiparticles

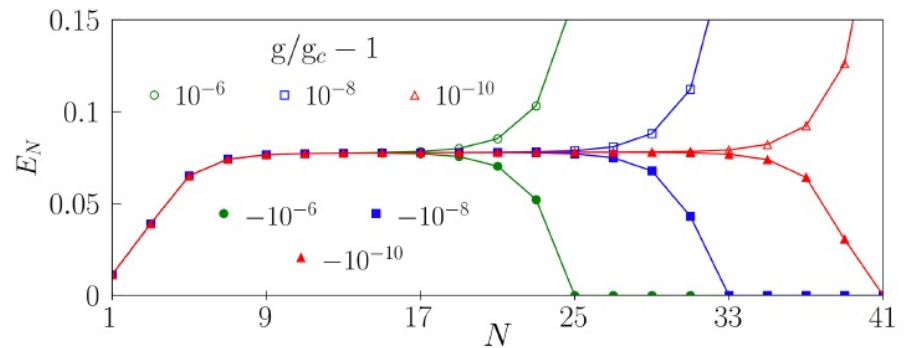
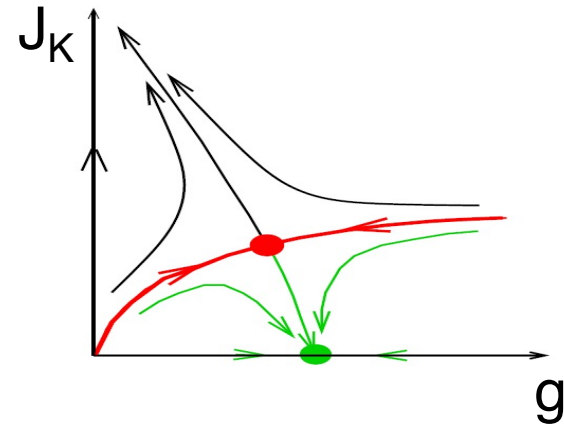


Quasiparticle weight $Z \rightarrow 0$



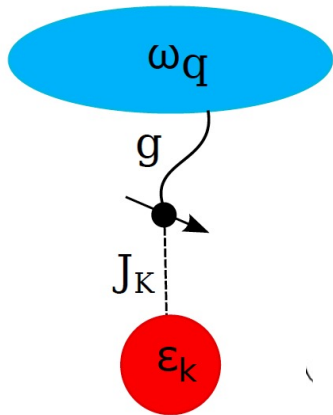
Critical spectrum at $g=g_c$ does not have a Fermi liquid form

RG via ϵ -expansion

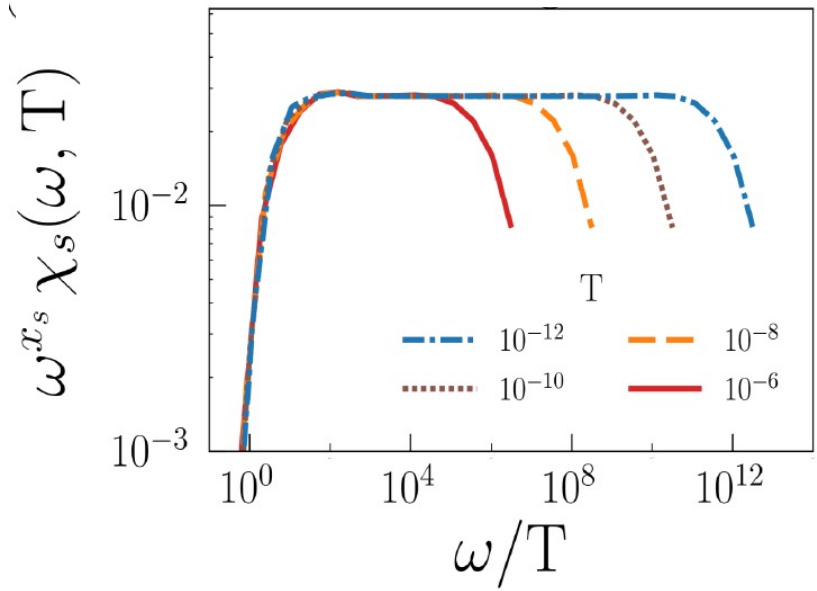


A.Kandala, H. Hu, QS, K. Ingersent,
arXiv:2206.01174

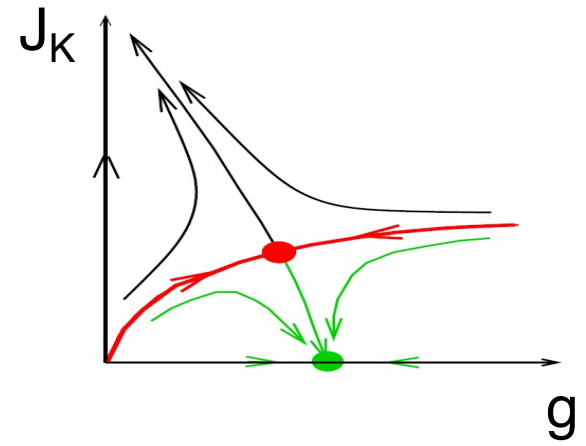
Interacting Fixed Point \rightarrow Dynamical Planckian ($\hbar\omega / k_B T$) Scaling



Quasiparticle weight $Z \rightarrow 0$

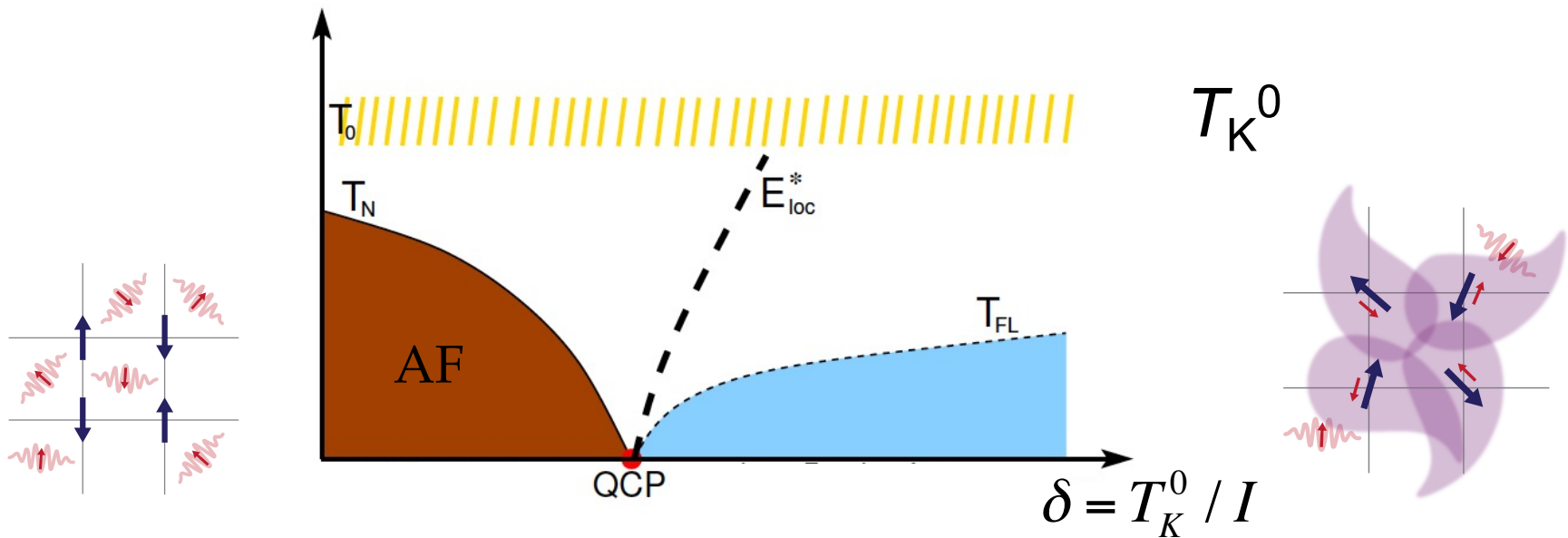


RG via ϵ -expansion



Kondo Destruction via EDMFT

Critical destruction of Kondo singlet
at the $T=0$ onset of antiferromagnetic order



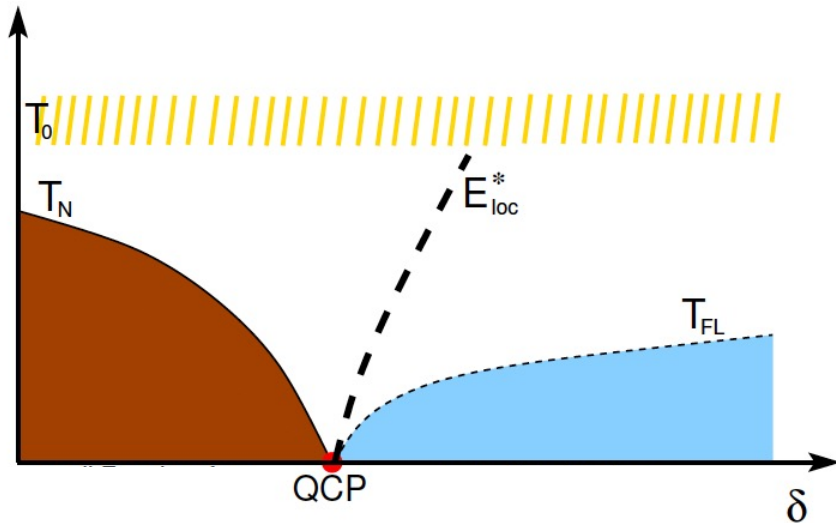
QS, S. Rabello, K. Ingersent & J. L. Smith, *Nature* 413, 804 (2001)

S. Kirchner, S. Paschen, Q. Y. Chen, S. Wirth, D. L. Feng,
J. D. Thompson, QS, *Rev. Mod. Phys.* 92, 011002 (2020)

Dynamical Scaling

Dynamical Planckian ($\hbar\omega/k_B T$) scaling:

$$\chi(\mathbf{Q}, \omega) \sim \frac{1}{(-i\hbar\omega)^\alpha} W^{-1} \left(\frac{\hbar\omega}{k_B T} \right)$$



--The QCP is interacting
(instead of Gaussian),
from Kondo destruction

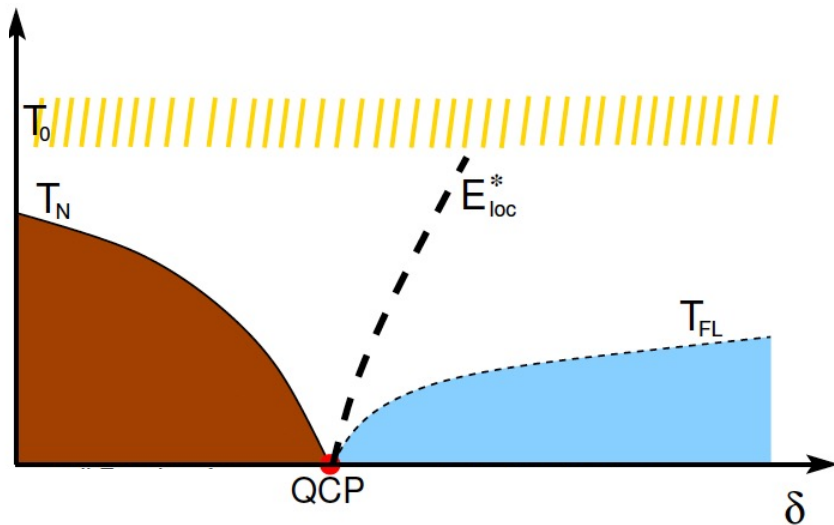
-- $k_B T$ is the only energy scale

QS, S. Rabello, K. Ingersent
& J. L. Smith, Nature 413, 804 (2001)

Dynamical Scaling

Dynamical Planckian ($\hbar\omega/k_B T$) scaling:

$$\chi(\mathbf{q}, \omega) \sim \frac{1}{(I_{\mathbf{q}} - I_{\mathbf{Q}}) + A(-i\hbar\omega)^\alpha W(\hbar\omega/k_B T)}$$



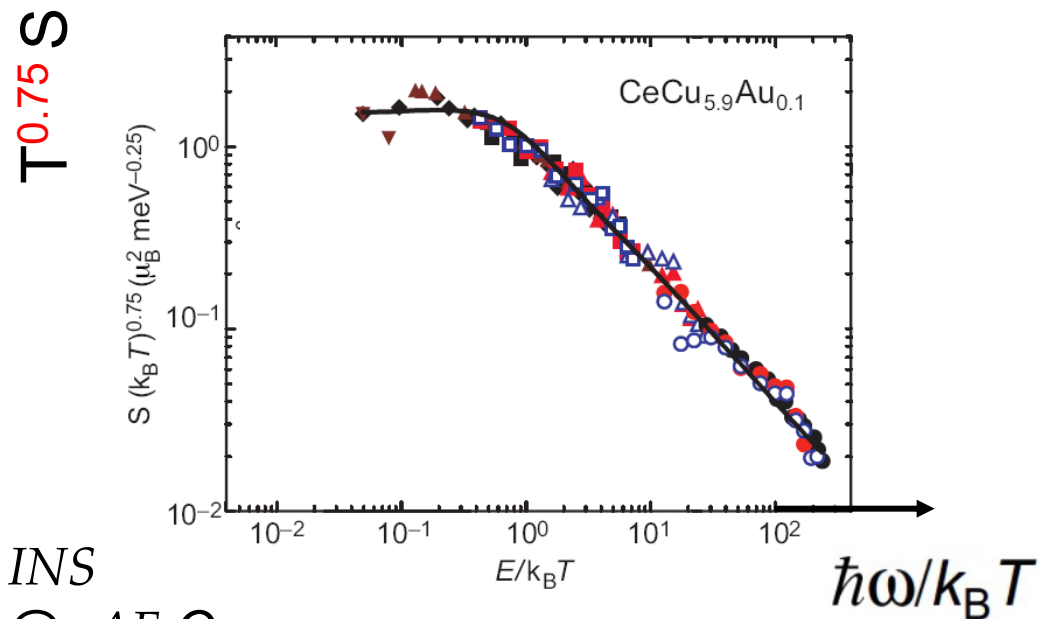
$$\alpha = 0.72-0.78$$

- D. Grepel & QS, PRL (2003)
- J-X Zhu, D. Grepel & QS, PRL (2003)
- M. Glossop & K. Ingersent, PRL (2007)
- J-X Zhu, S. Kirchner, R. Bulla, QS, PRL (2007)

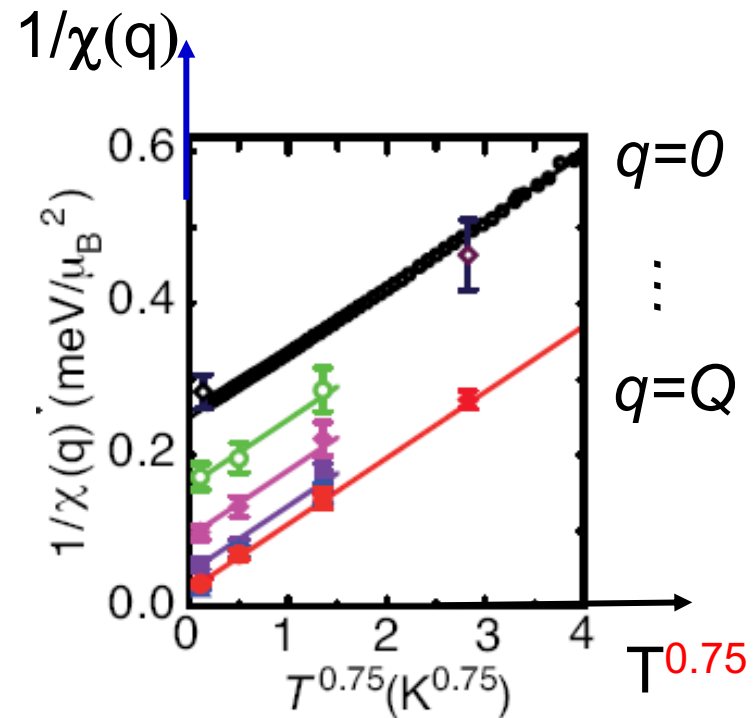
QS, S. Rabello, K. Ingersent
& J. L. Smith, Nature 413, 804 (2001)

Dynamical Scaling of Spin Responses in $\text{CeCu}_{5.9}\text{Au}_{0.1}$

Fractional exponent $\alpha=0.75-0.80$



INS
@ AF Q



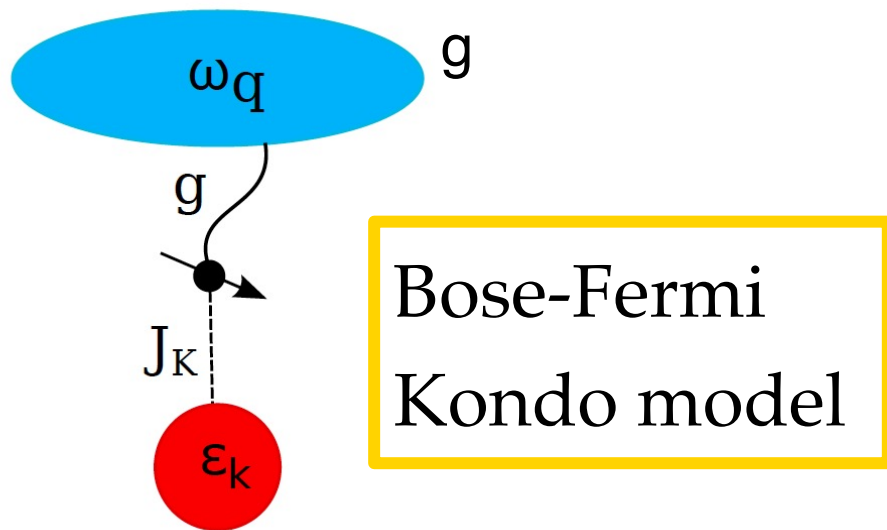
INS and M/H

inelastic neutron scattering expts:

A. Schröder et al. ($\text{CeCu}_{5.9}\text{Au}_{0.1}$);

M. Aronson et al.

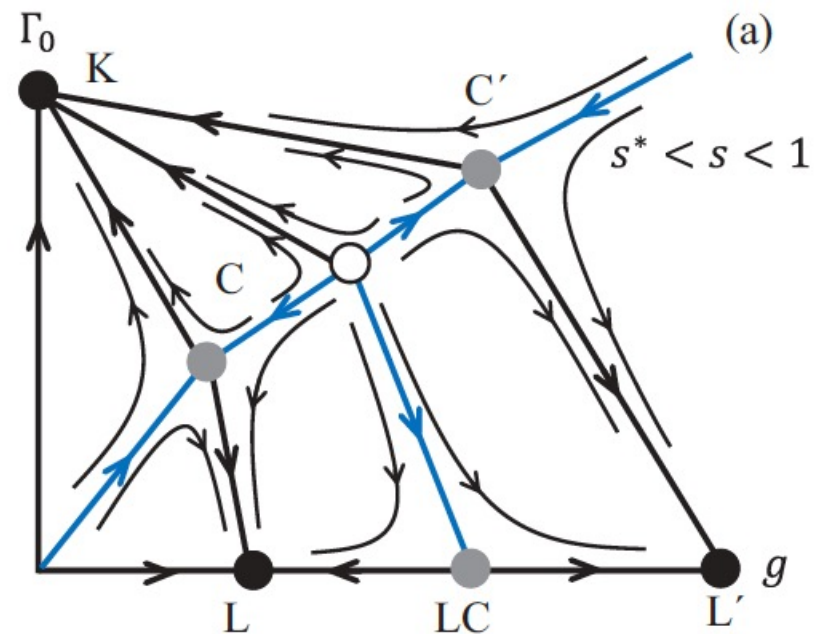
SU(2)-symmetric Model



(Fixed-point annihilation)

RG flow:

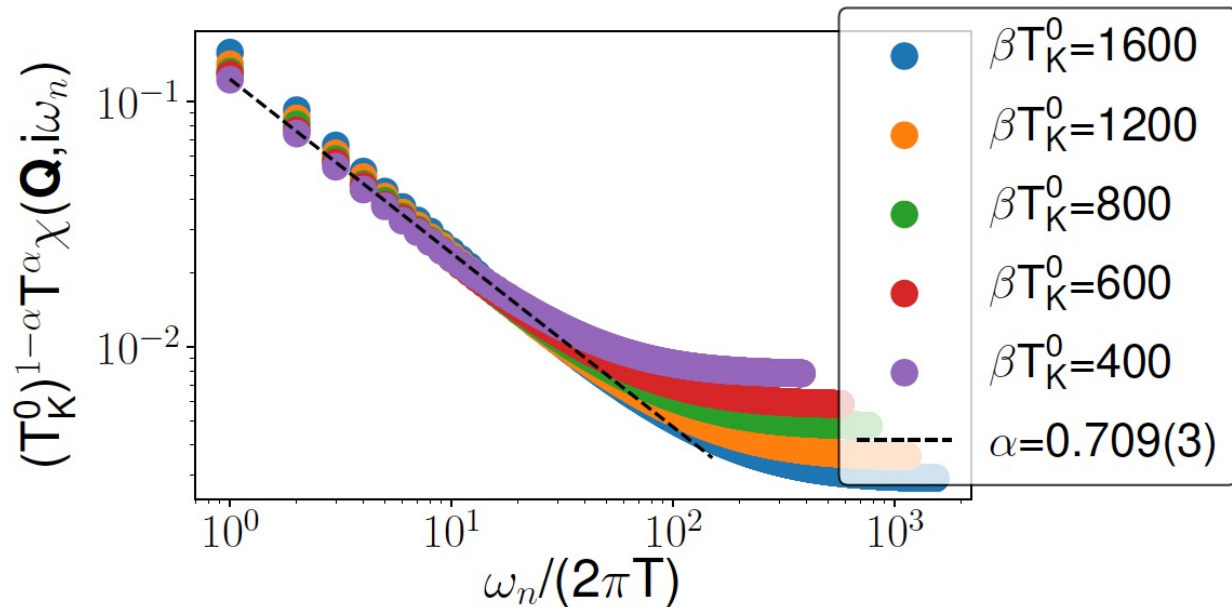
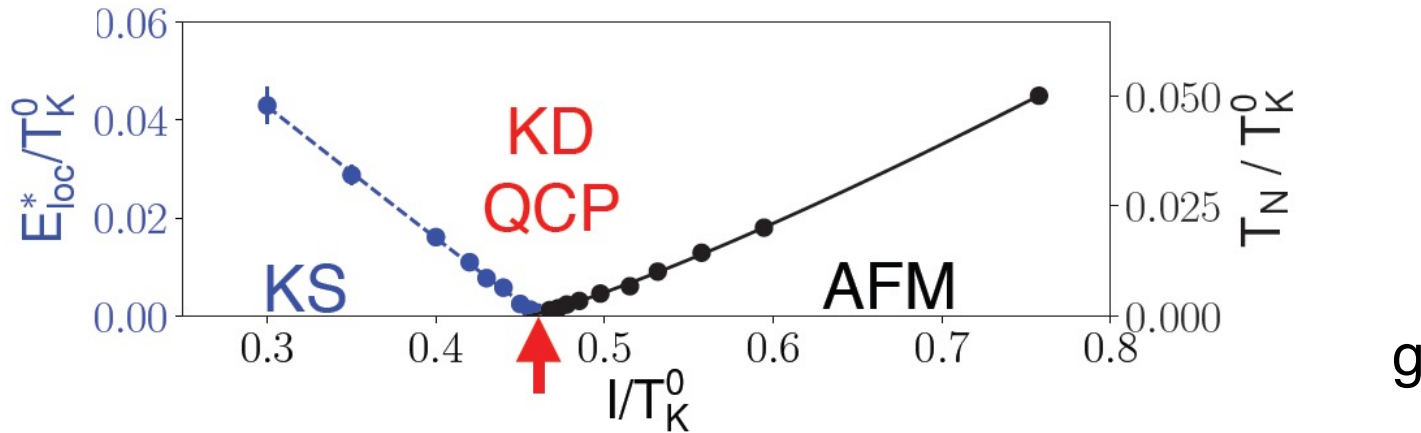
$$(1-\varepsilon \equiv s)$$



A.Cai & QS, Phys. Rev. B100, 014439
(2019)

See also A. Nahum, arXiv:2202.08431

SU(2) Kondo Lattice: Loss of Quasiparticles, and Dynamical Quantum Scaling



H. Hu, A. Cai
& QS (2020)

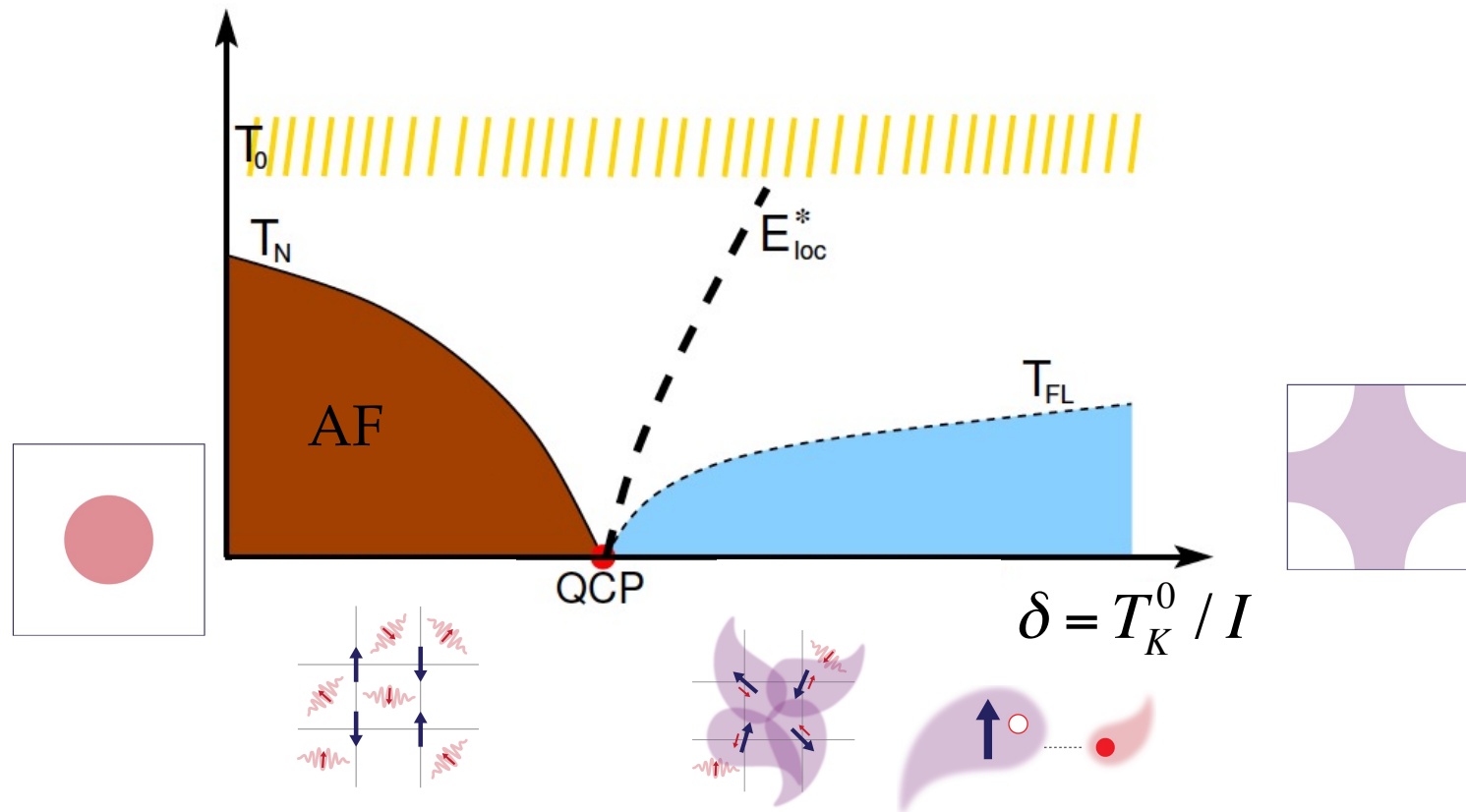
Kondo Destruction



**“Large”-to-“Small” Fermi
Surface Fluctuations**

Quantum Criticality from Kondo Destruction

Sudden reconstruction of
Fermi surface from large to small



QS, S. Rabello, K. Ingersent & J. L. Smith, Nature 413, 804 (2001)

Quantum Criticality from Kondo Destruction

- Loss of quasiparticles via the suppression of the Kondo-destruction energy scale E_{loc}^*
- Suppression of the Kondo scale \leftrightarrow the suppression of a pole in the conduction-electron self-energy:

$$\Sigma(\mathbf{k}, \omega) = \frac{(b^*)^2}{\omega - \varepsilon_f^*}$$

QS, S. Rabello, K. Ingersent & J. L. Smith, Nature 413, 804 (2001)

Quantum Criticality from Kondo Destruction

- Loss of quasiparticles via the suppression of the Kondo-destruction energy scale E_{loc}^*
- Suppression of the Kondo scale \leftrightarrow the suppression of a pole in the conduction-electron self-energy:

$$\Sigma(\mathbf{k}, \omega) = \frac{(b^*)^2}{\omega - \varepsilon_f^*}$$

- Kondo destruction—Prediction: large-to-small Fermi surface transformation across the QCP

QS, S. Rabello, K. Ingersent & J. L. Smith, Nature 413, 804 (2001)

Quantum Criticality from Kondo Destruction

➤ Fermi-surface jump based on Hall measurements (YbRh_2Si_2 , $\text{Ce}_3\text{Pd}_{20}\text{Si}_6$):

S. Paschen, T. Luhmann, S. Wirth, P. Gegenwart, O. Trovarelli, C. Geibel, F. Steglich, P. Coleman, QS, Nature 432, 881 (2004)

S. Friedemann, N. Oeschler, S. Wirth, C. Krellner, C. Geibel, F. Steglich, S. Paschen, S. Kirchner, and QS, PNAS 107, 14547 (2010)

P. Gegenwart, T. Westerkamp, C. Krellner, Y. Tokiwa, S. Paschen, C. Geibel, F. Steglich, E. Abrahams, QS, Science 315, 969 (2007)

V. Martelli, A. Cai, E. M. Nica, M. Taupin, A. Prokofiev, C. C. Liu, H.-H. Lai, R. Yu, K. Ingersent, R. Kuchler, A. M. Strydom, D. Geiger, J. Haenel, J. Larrea, QS, S. Paschen, PNAS 116, 17701 (2019).

➤ Fermi-surface jump based on quantum oscillations (CeRhIn_5):

H. Shishido, R. Settai, H. Harima, & Y. Onuki, JPSJ 74, 1103 ('05)

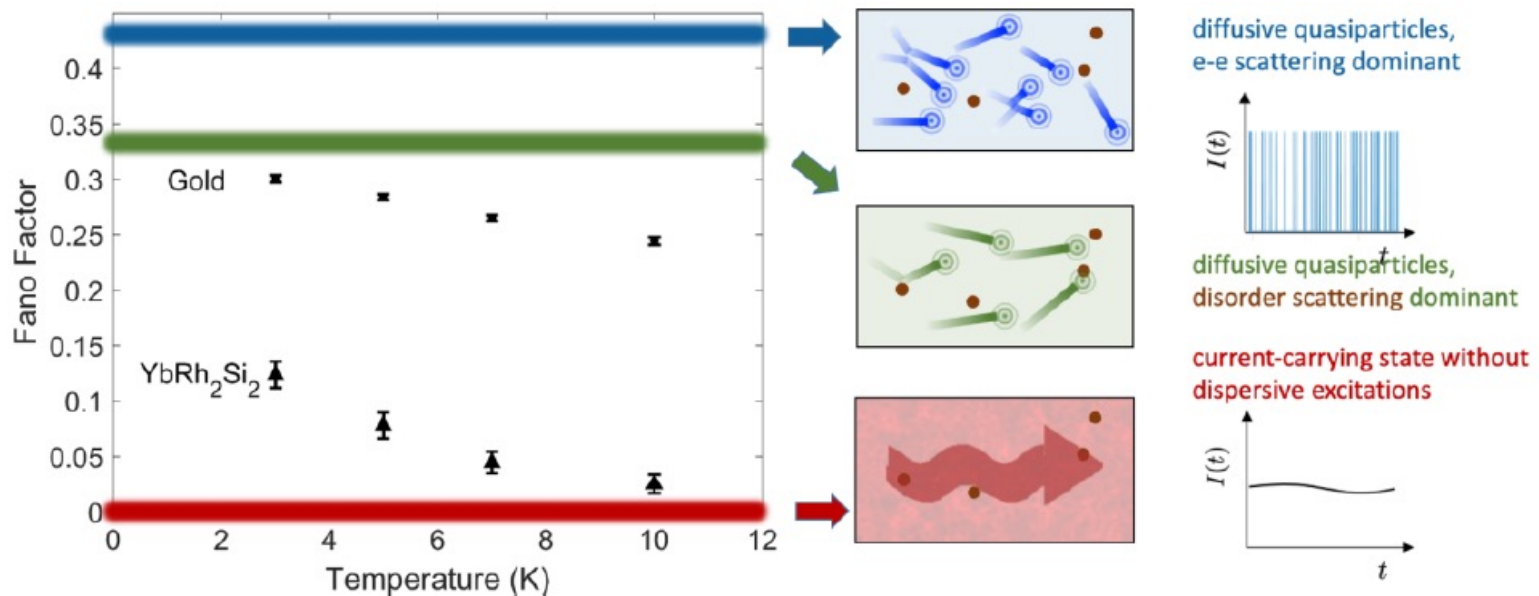
L. Jiao, Y. Chen, Y. Kohama, D. Graf, E. D. Bauer, J. Singleton, J.-X. Zhu, Z. F. Weng, G. M. Pang, T. Shang, J. L. Zhang, H. O. Lee, T. Park, M. Jaime, J. D. Thompson, F. Steglich, QS, H. Q. Yuan, PNAS 112, 673 (2015).

Quantum Criticality from Kondo Destruction

- Fermi-surface jump based on Hall measurements
(YbRh_2Si_2 , $\text{Ce}_3\text{Pd}_{20}\text{Si}_6$)
- Fermi-surface jump based on quantum oscillations
(CeRhIn_5)
- Cf. Status report on Fermi-surface jump and localization-delocalization across the QCP:
“**Heavy-electron quantum criticality and single-particle spectroscopy**”,
S. Kirchner, S. Paschen, Q. Chen, S. Wirth, D. L. Feng, J. D. Thompson, QS,
[Rev. Mod. Phys. 92, 011002 \(2020\)](#).

Quantum Criticality from Kondo Destruction

- Fermi-surface jump based on Hall measurements
- Fermi-surface jump based on quantum oscillations
- **Loss of quasiparticles: Shot-noise reduction**



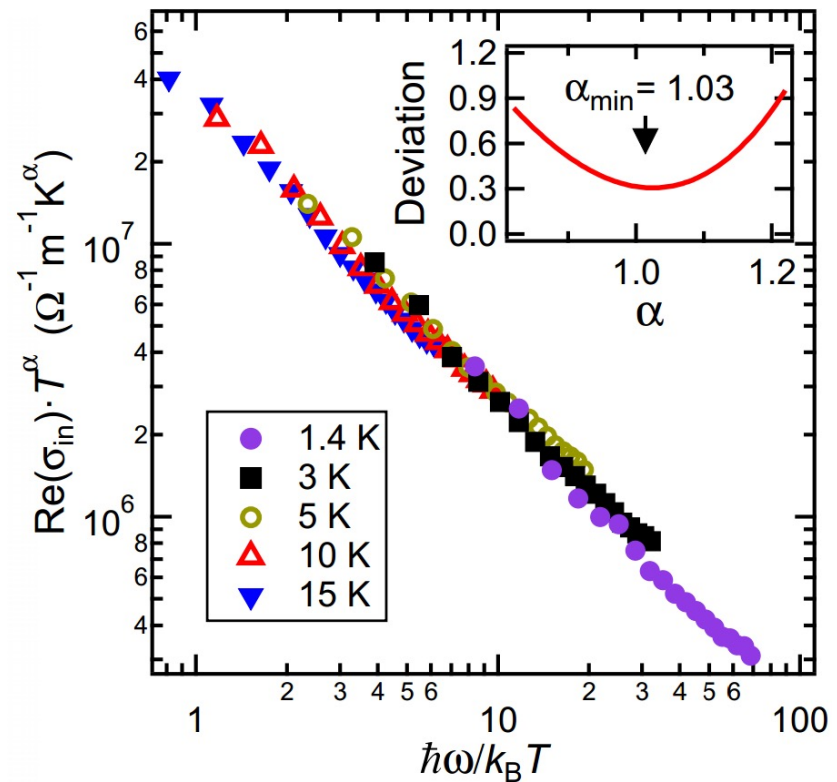
L. Chen, D. T. Lowder, E. Bakali, A. M. Andrews, W. Schrenk, M. Waas, R. Svagera, G. Eguchi, L. Prochaska, QS, S. Paschen, D. Natelson, arXiv:2206.00673

Charge Response with Dynamical Scaling

Singular charge fluctuations at a magnetic quantum critical point

L. Prochaska^{1*}, X. Li^{2*†}, D. C. MacFarland^{1,3*‡}, A. M. Andrews³, M. Bonta⁴, E. F. Bianco^{5§}, S. Yazdi^{6¶},
 W. Schrenk⁷, H. Detz^{7#}, A. Limbeck⁴, Q. Si⁸, E. Ringe^{6**}, G. Strasser^{3,7}, J. Kono^{2,6,8}, S. Paschen^{1,8††}

$\hbar\omega/k_B T$ scaling of
 optical conductivity



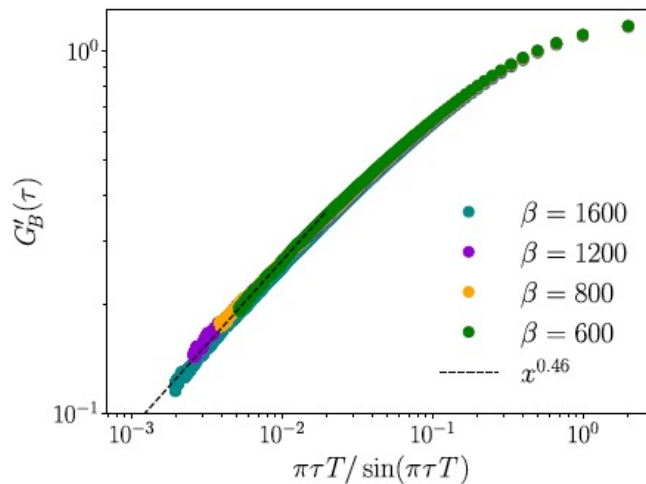
Science 367, 285 (2020)

Dynamical Quantum Scaling of Charge Response at a Kondo-destruction QCP

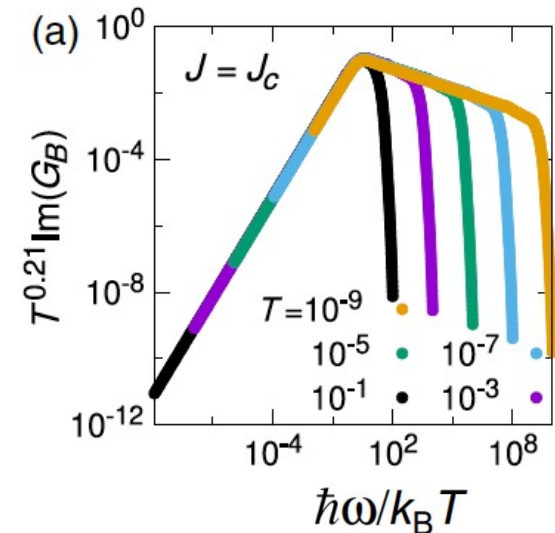
$$J_K \sum_{\alpha} S \cdot s_{\alpha} = J_K \sum_{\sigma\sigma'} (f_{\sigma}^{\dagger} f_{\sigma'} - \delta_{\sigma\sigma'}) c_{\alpha\sigma'}^{\dagger} c_{\alpha\sigma} \xrightarrow{\text{H.S. transform}} B_{\alpha}^{\dagger} \sum_{\sigma} c_{\alpha\sigma}^{\dagger} f_{\sigma} + h.c.$$

Chargon

Kondo lattice via EDMFT SU(2):



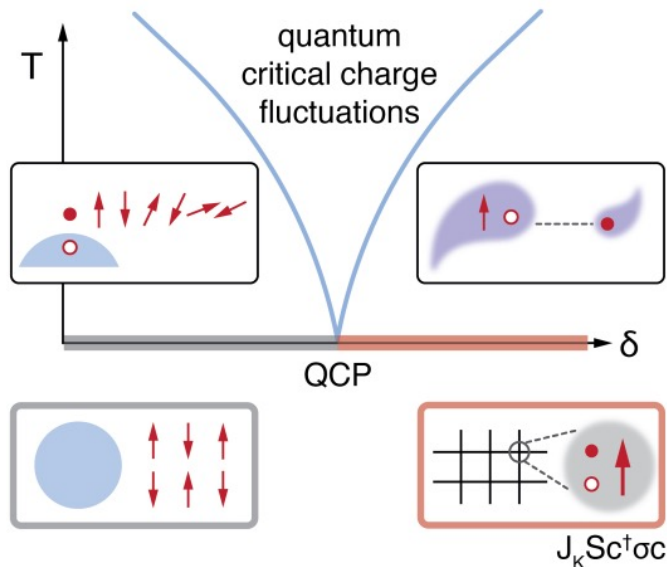
BFK model at large-N:



Dynamical Quantum Scaling of Charge Response at a Kondo-destruction QCP

Qualitative picture:

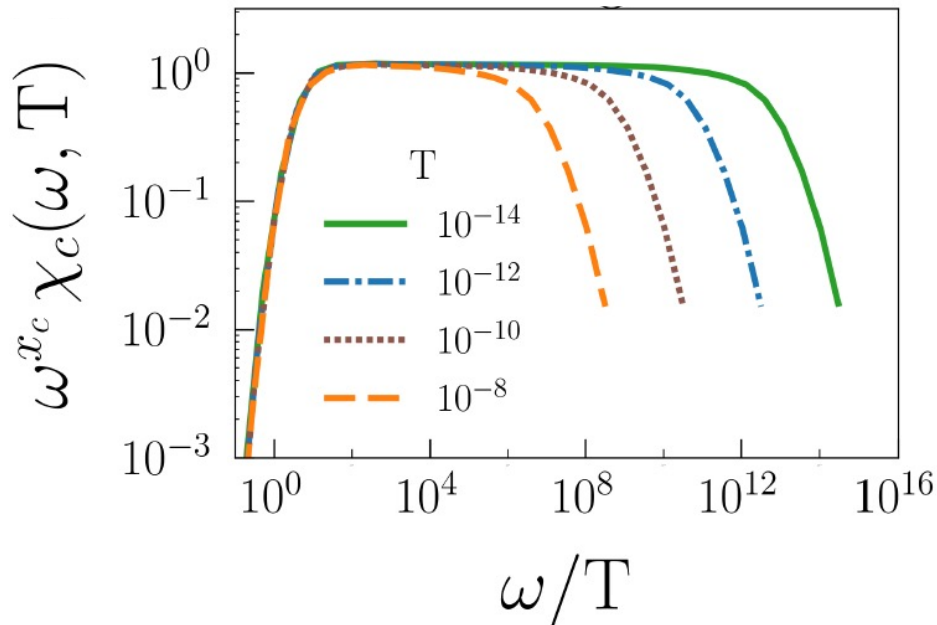
- QCP involves the destruction of Kondo singlet: localization-delocalization of f electrons
→ electronic d.o.f. is critical
 - Interacting QCP
- } → Charge response also satisfies $\hbar\omega/kBT$ scaling



- Captures a dynamical Kondo effect at the Kondo-destruction QCP
- Implications for superconductivity

Dynamical Quantum Scaling of Charge Response at a Kondo-destruction QCP

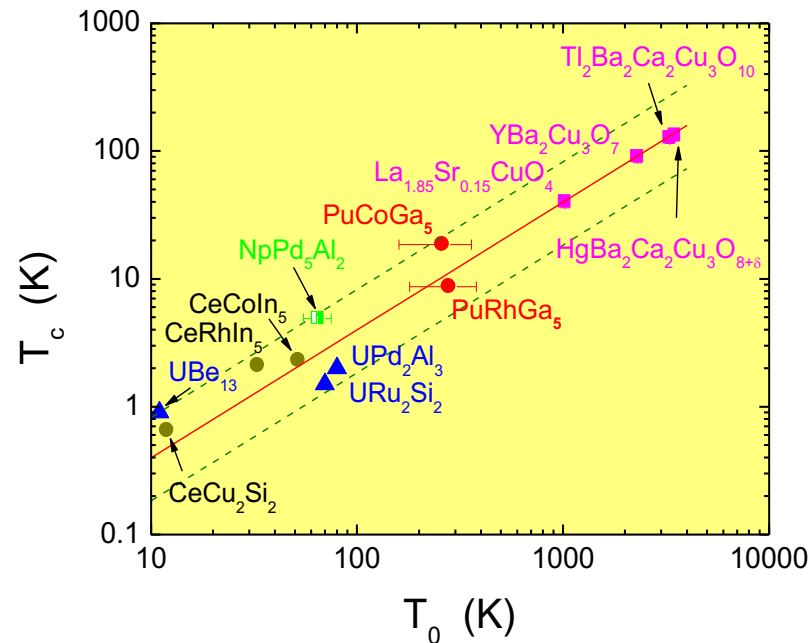
The regime of particle-hole asymmetry (Bose-Fermi Anderson, mixed-valence) (the case for CeRhSn, CeIrSn)



A. Kandala, H. Hu, QS, K. Ingersent, arXiv:2206.01174

**From Loss of Quasiparticles
to
High T_c Superconductivity**

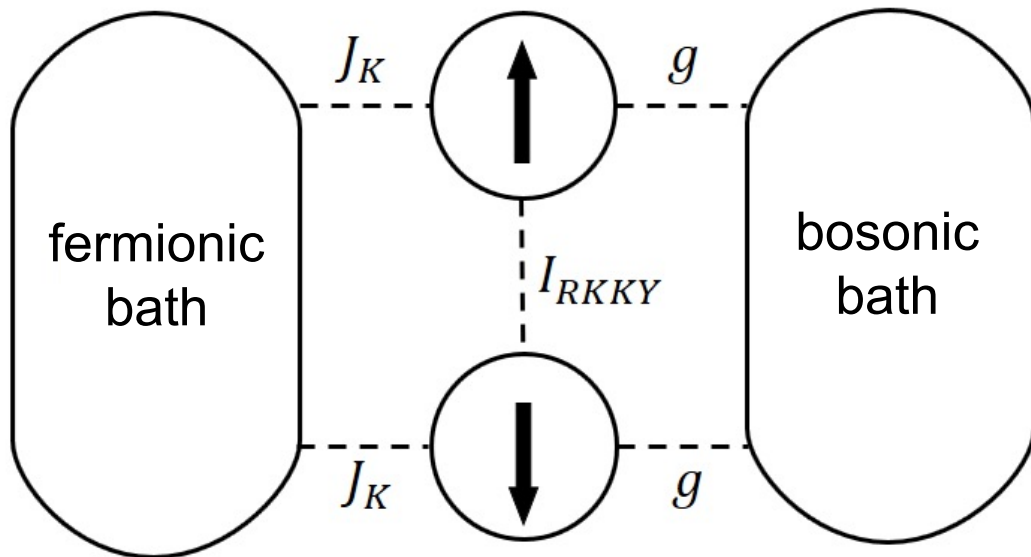
- Heavy-fermion superconductivity: ~50 members
- Most of them with antiferromagnetic correlations
- Modern understanding of quantum criticality has not been treated in driving superconductivity



Cluster-EDMFT

$$H = \sum_{i,j,\sigma} t_{ij} (c_{i\sigma}^\dagger c_{j\sigma} + \text{h.c.}) + \sum_i (\epsilon_f n_{fi} + U n_{fi\uparrow} n_{fi\downarrow}) \\ + \sum_{i,\sigma} (V c_{i\sigma}^\dagger f_{i\sigma} + \text{h.c.}) + \sum_{i,j} I_{ij} \mathbf{S}_{fi} \cdot \mathbf{S}_{fj}$$

Cluster-EDMFT

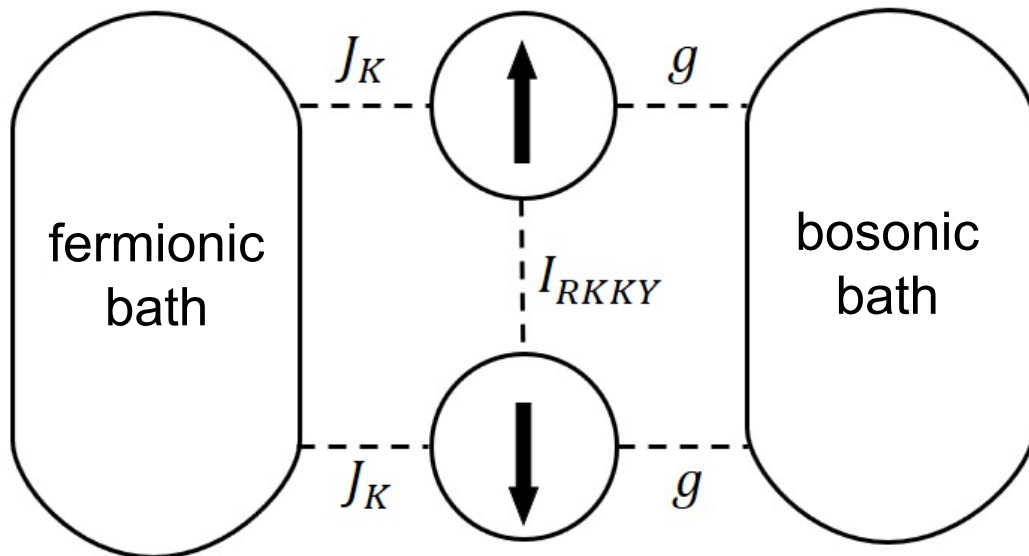
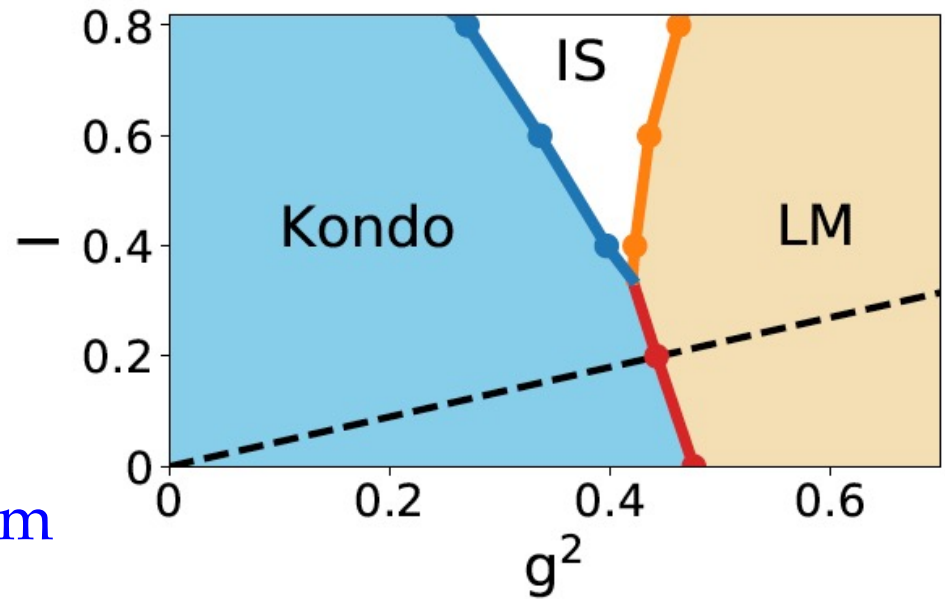


J. Pixley, A. Cai & QS,
PRB 91, 125127 (2015)

Cluster-EDMFT

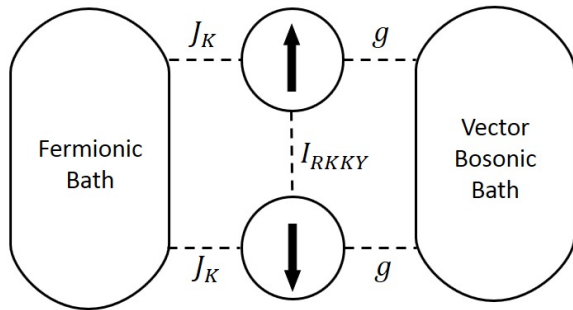
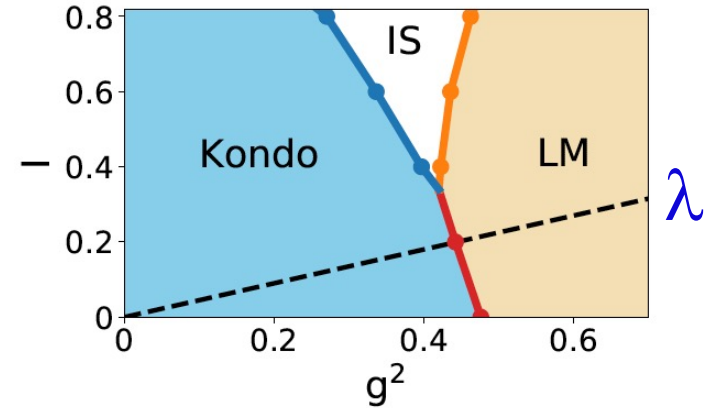
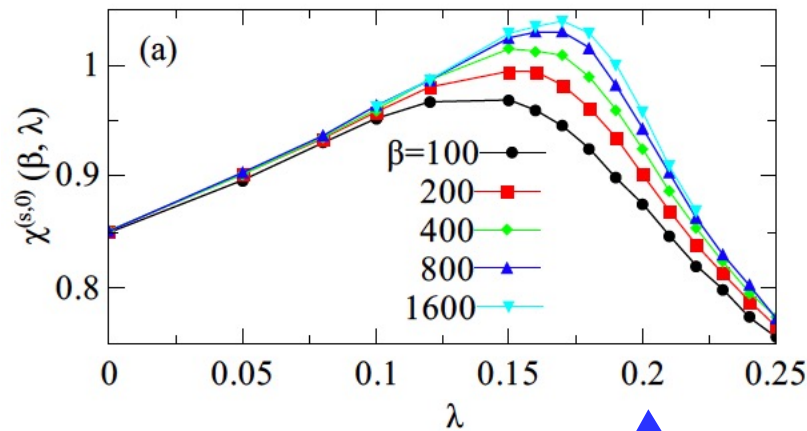
RKKY interaction generates spin-singlet correlations:

- bond-singlet correlations everywhere
- “intersite-singlet (IS)” regime in the phase diagram



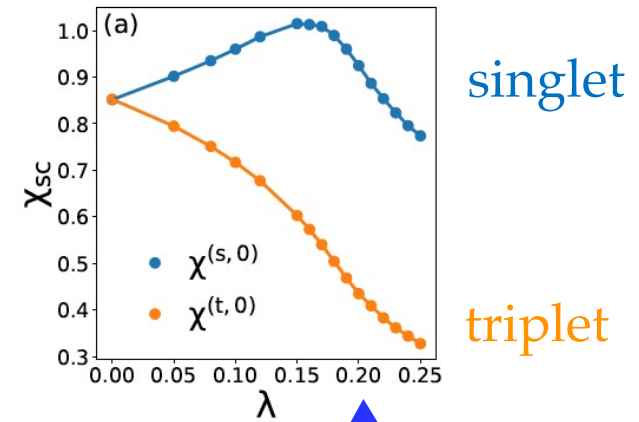
Pairing Correlations from RKKY Interactions

Spin-singlet pairing correlation



KD
QCP

SU(2)

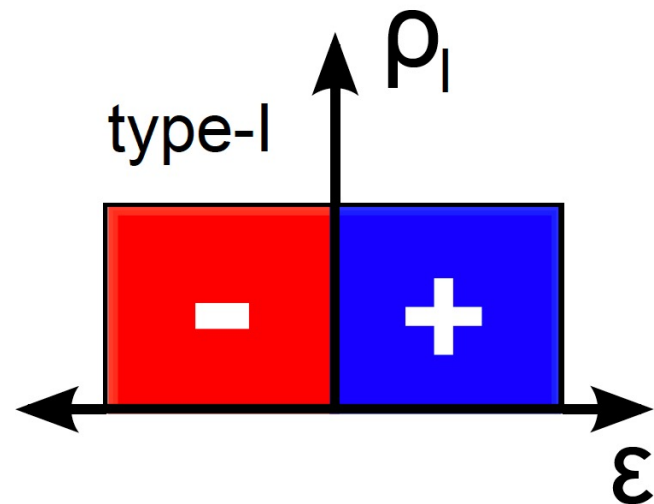
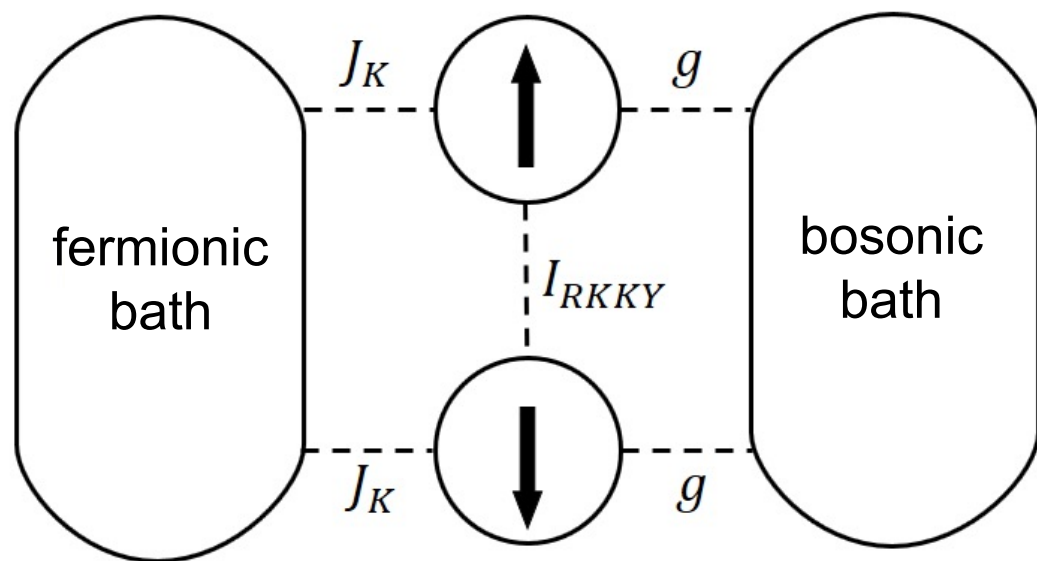


KD QCP

Cluster-EDMFT

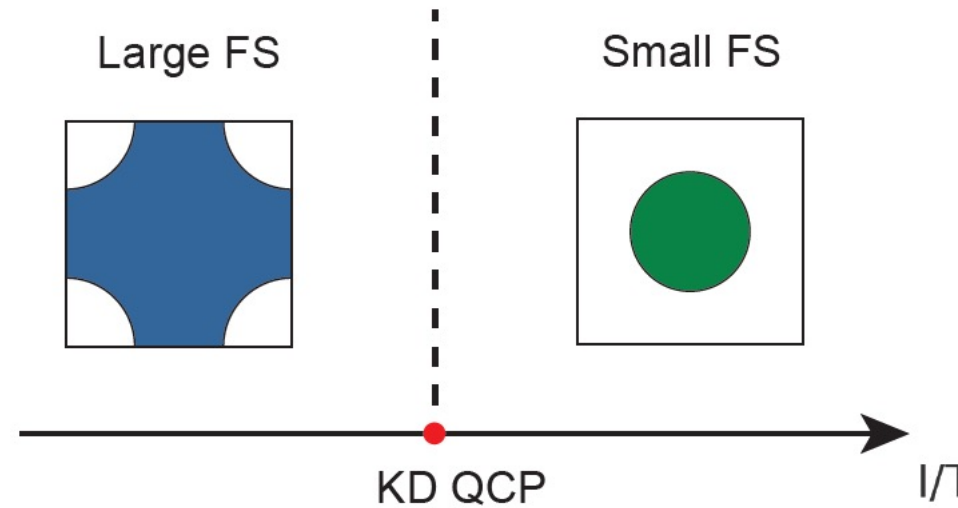
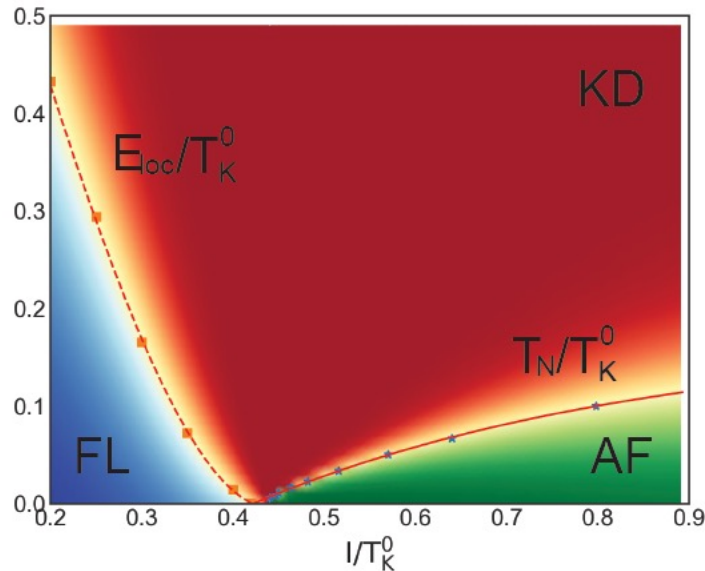
- Type I model

$$\chi_{loc}^{\alpha}(i\omega) = \sum_q \frac{1}{I_q + M^{\alpha}(i\omega)} = \int_{-\infty}^{\infty} \frac{\rho_I(\epsilon)}{\epsilon + M^{\alpha}(i\omega)} d\epsilon$$



Kondo-destruction QCP

- Type I model



Cluster-EDMFT

EDMFT result robust: loss of quasiparticles at the QCP

H. Hu, A. Cai, L. Chen, L. Deng, J. Pixley, K. Ingersent & QS,

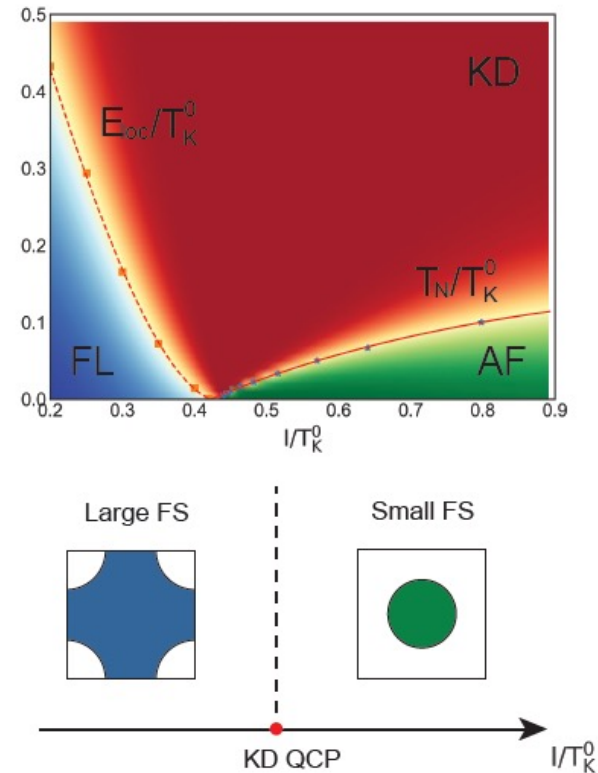
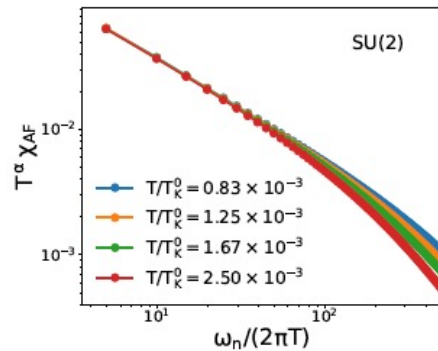
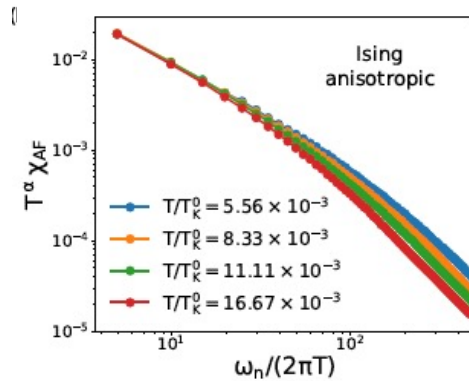
arXiv:2109.13224

Kondo-destruction Quantum Critical Metal

Kondo-destruction quantum criticality:
dynamical scaling is robust

$$\chi_{AF}(T) \sim T^{-\alpha}$$

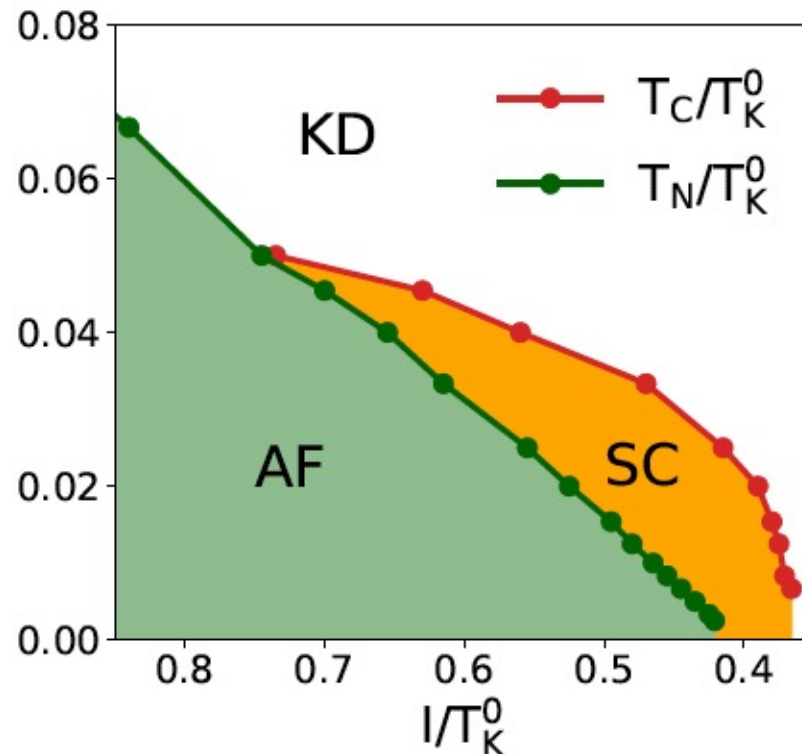
$$\alpha = 0.81(4)$$



H. Hu, A. Cai, L. Chen, L. Deng, J. Pixley, K. Ingersent & QS,

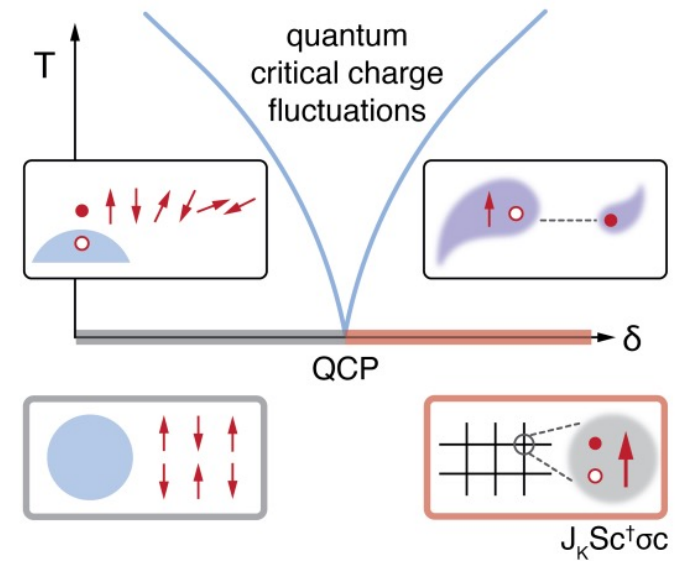
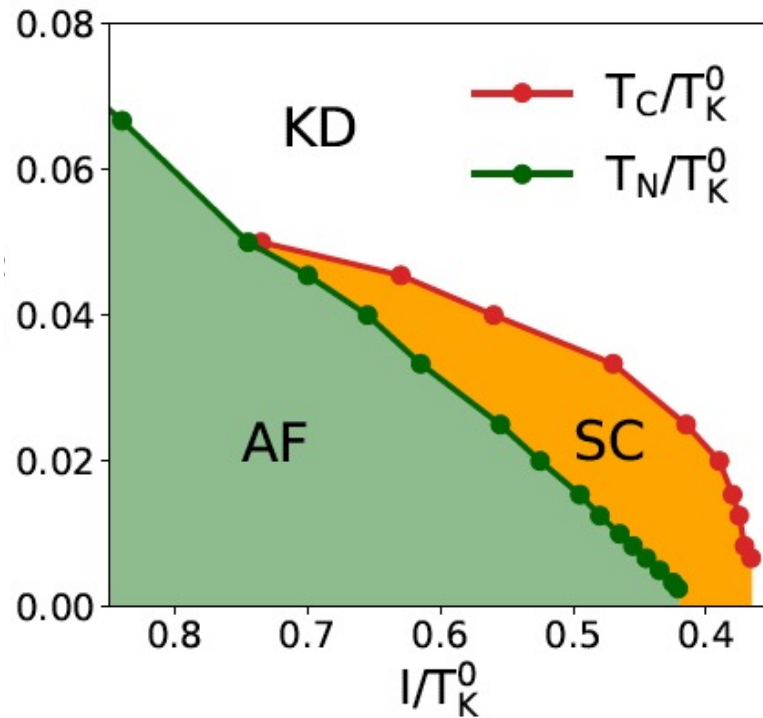
arXiv:2109.13224

Development of Superconductivity



H. Hu, A. Cai, L. Chen, L. Deng, J. Pixley, K. Ingersent & QS,
arXiv:2109.13224

Development of Superconductivity



Superconductivity
driven by
Fermi surface fluctuations

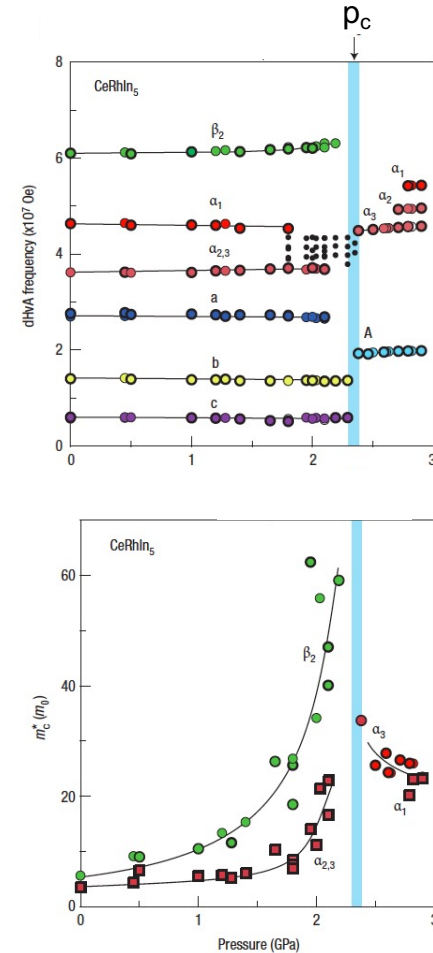
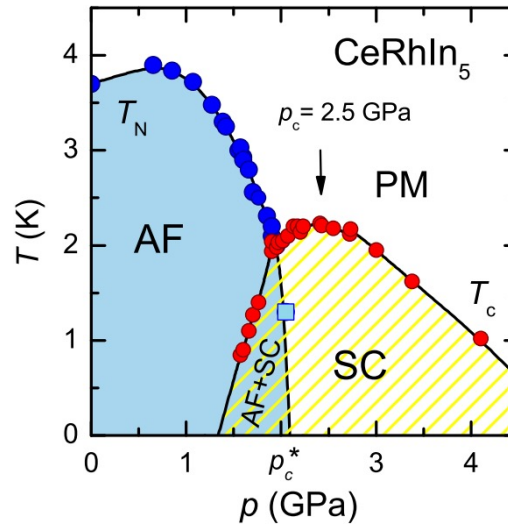
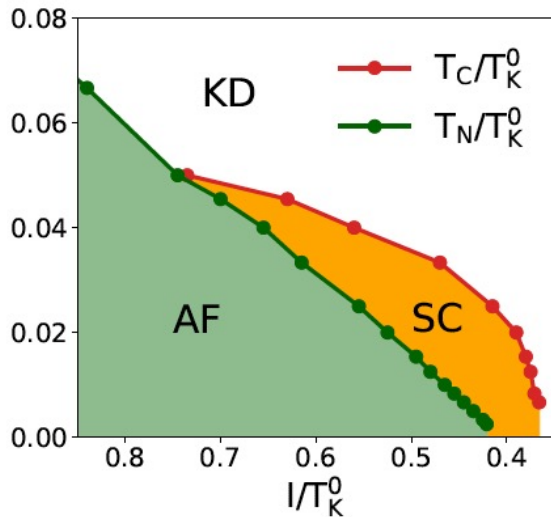
H. Hu, A. Cai, L. Chen, L. Deng, J. Pixley, K. Ingersent & QS,

arXiv:2109.13224

Superconductivity near Kondo-destruction QCP in CeRhIn₅

high T_c :

$$T_c/T_K^0 \approx 0.03$$



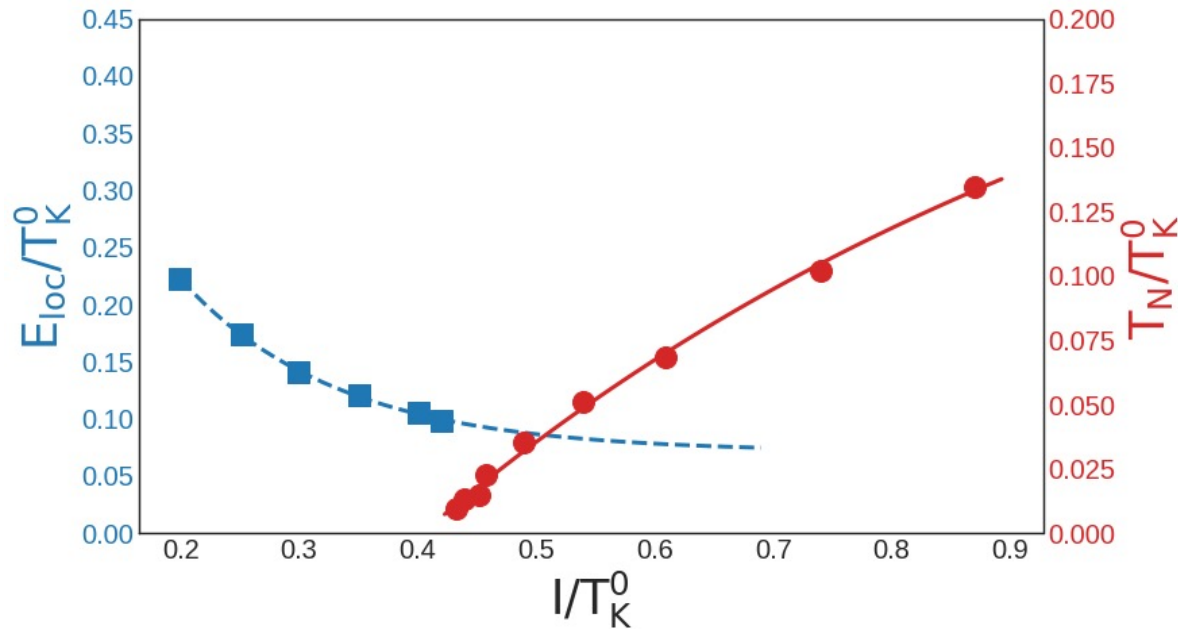
T. Park et al., Nature (2006);

G. Knebel et al., PRB (2006)

H. Shishido et al., JPSJ (2005)

SDW_r QCP

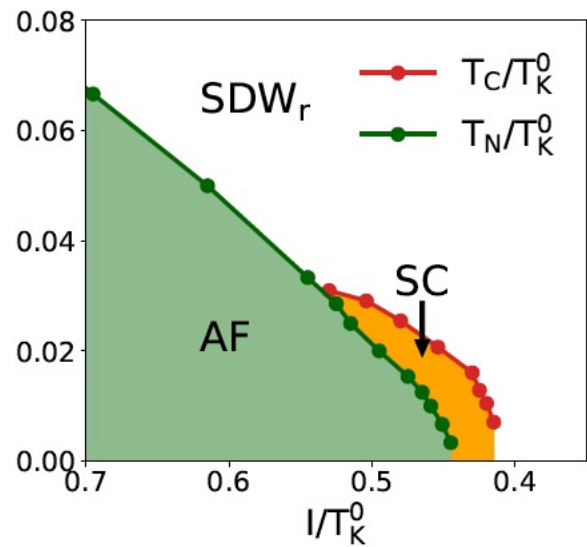
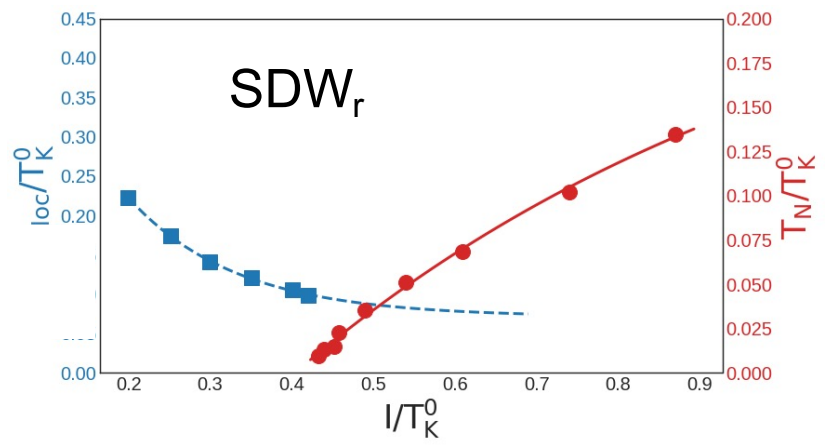
- Type II model: SDW_r QCP



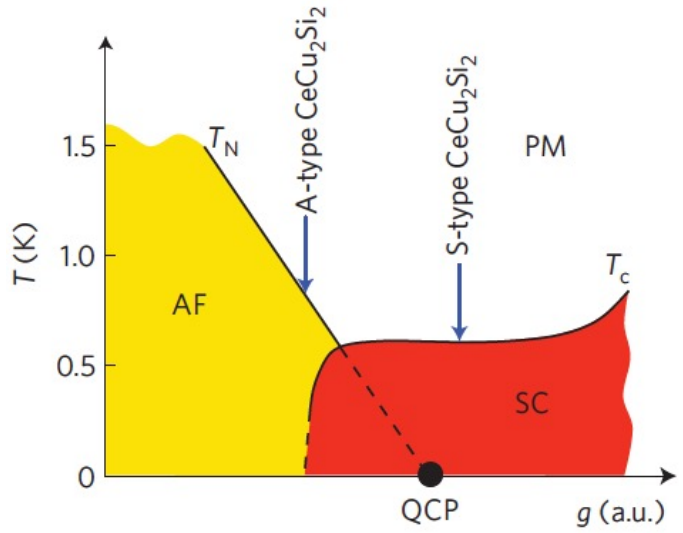
- Loss of quasiparticles over an extended dynamical range

L. Chen, H. Hu, QS,
unpublished (2022)

Superconductivity w/ a large dynamical range of Fermi-surface fluctuations in CeCu₂Si₂



$T_c/T_K^0 \approx 0.02$

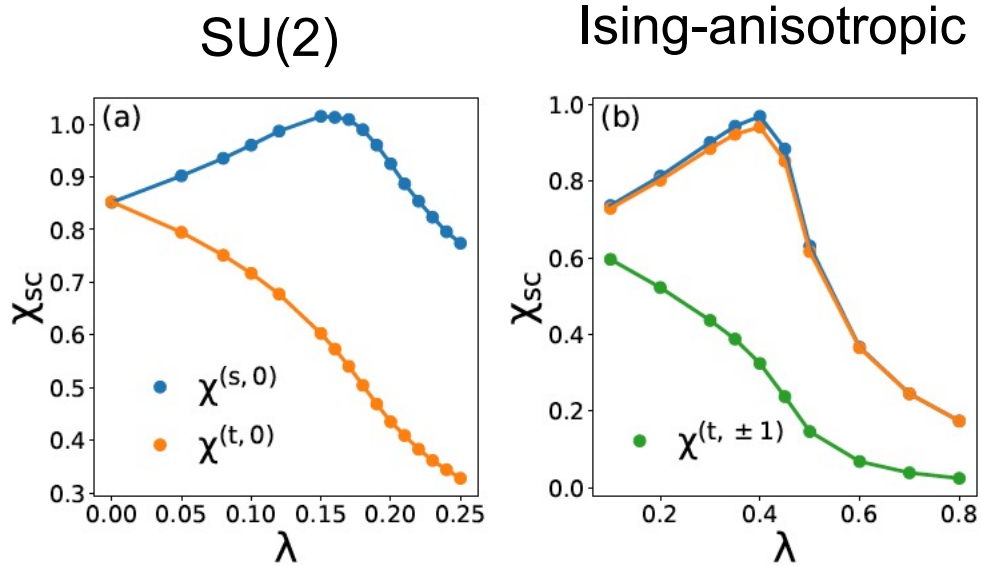


$T_{cr} \sim 1 K$

$T_K^0 \sim 20 K$

Route towards Spin-Triplet Pairing

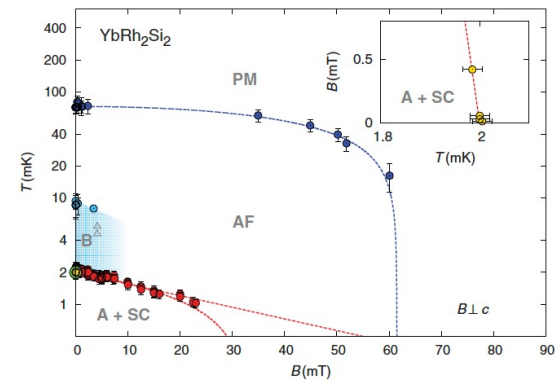
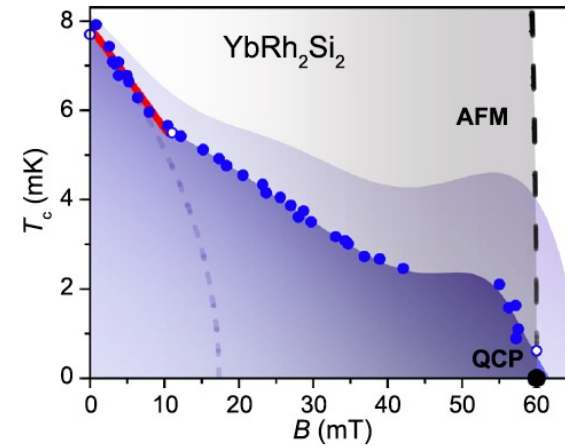
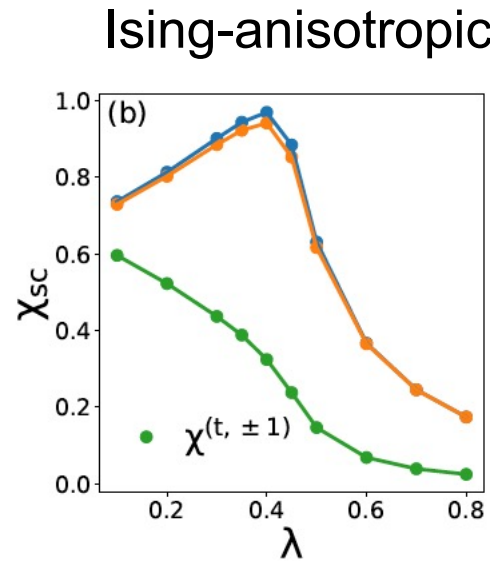
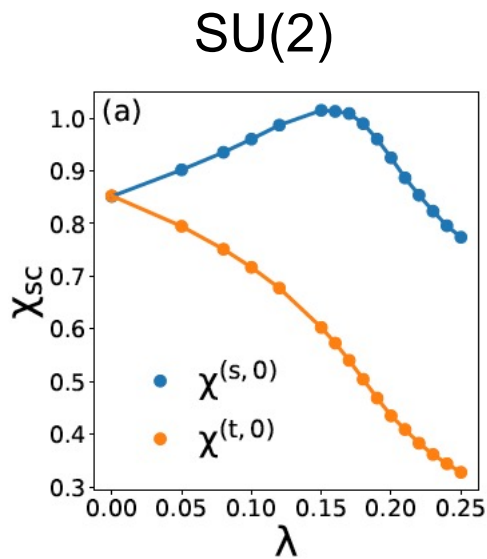
Cluster Bose-Fermi Anderson models:



H. Hu, A. Cai, L. Chen & QS,
arXiv:2109.12794

Route towards Spin-Triplet Pairing

YbRh₂Si₂ as a candidate setting:



H. Hu, A. Cai, L. Chen & QS,
arXiv:2109.12794

D. H. Nguyen et al.,
Nat. Comm. (2021)

E. Schuberth et al.,
Science (2016)

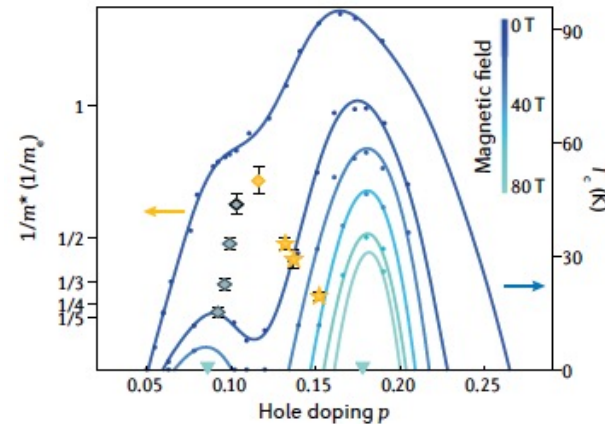
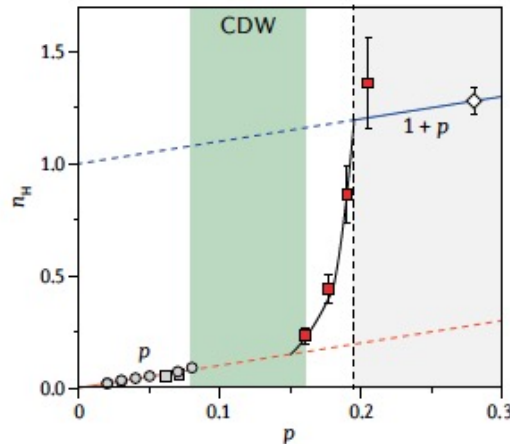
Broader Contexts

Quantum critical electrons bordering localization

-- Cf. connection w/ other correlated systems

S. Badoux et al ('16)

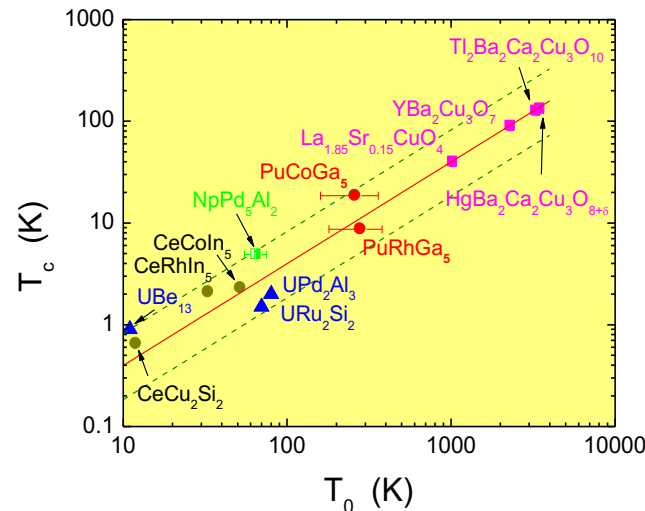
Y. Fang et al ('22)



B. J. Ramshaw et al ('15)

See also

F. Balakirev et al ('03)



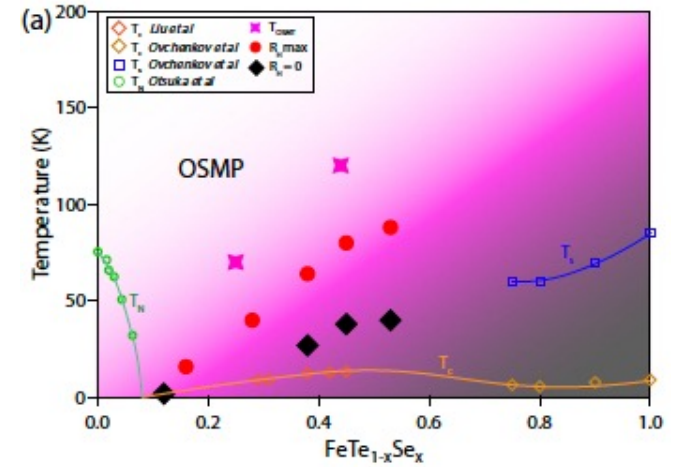
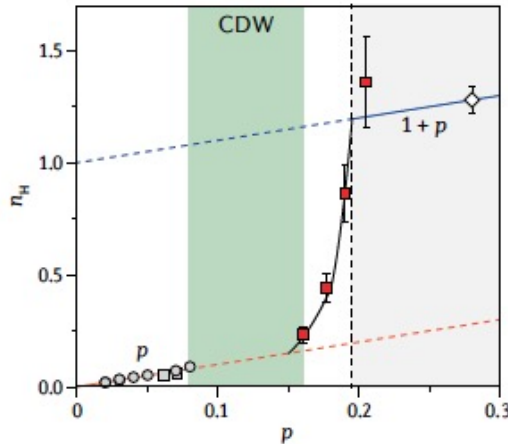
Broader Contexts

Quantum critical electrons bordering localization

-- Cf. connection w/ other correlated systems

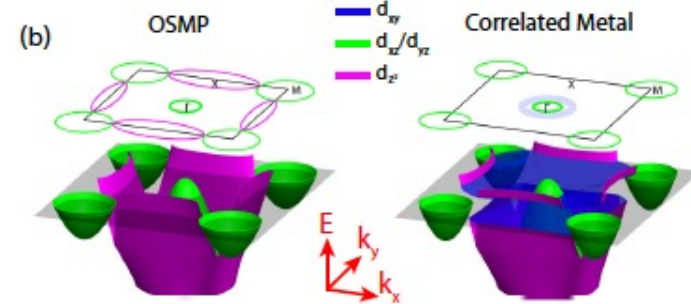
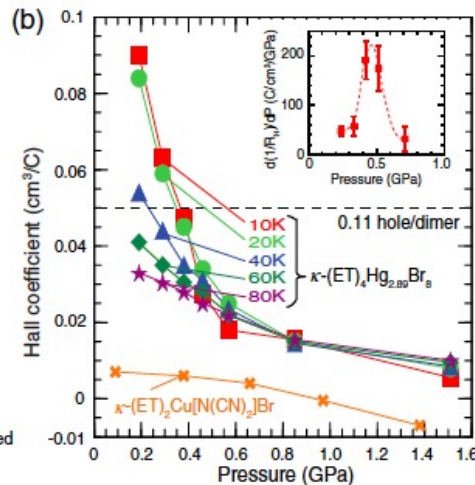
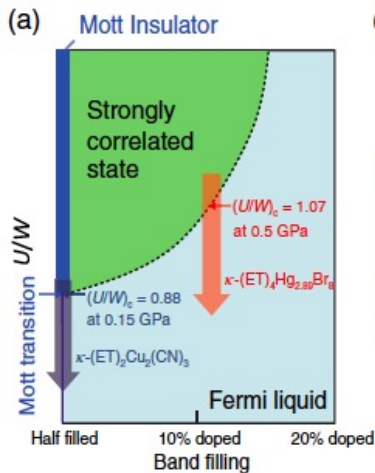
S. Badoux et al ('16)

Y. Fang et al ('22)



H. Oike et al. ('15)

K. Wakamatsu et al. ('22)



J. Huang et al. ('22)

SUMMARY

- **Quantum criticality from Kondo destruction:**
 - Loss of quasiparticles; dynamical Planckian scaling
 - Jump of Fermi surface from large to small
- **Singular charge response with $\hbar\omega/k_B T$ scaling:**
 - Captures the dynamical Kondo effect
- **Superconductivity of the QC metal:**
 - Kondo destruction (CeRhIn_5) and SDW_r (CeCu_2Si_2)
 - Route towards spin-triplet pairing (maybe YbRh_2Si_2)

Overview materials:

--S. Paschen and QS, Nat. Rev. Phys. 3, 9 (2021)

--S. Kirchner et al, Rev. Mod. Phys. 92, 011002 (2020)

